

Chapter 1 Introduction

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1.1 Embedded System

Embedded system is an optimized computing system consisting of the mechanical or electrical system, often with real time computing constraints designed for performing some dedicated functions.

The common characteristics of embedded system are as follows:-

1) Single Functioned

An embedded system is designed to perform specific tasks repeatedly. Newer program version update can be done in some rare cases.

2) Tightly Constrained

An embedded system have tightly constrained design metrics such as low cost, portable size, high performance, limited power consumption and so on.

3) Reactive and real time

An embedded system should continuously react to changes in the system's environment and should provides output in a real time within a specified time frame. Delayed computation may result in system failure.

For eg: digital camera.

- It is designed to capture image or videos repeatedly.
- It is cheap, single chip system, small in size and low power system.
- It is reactive to some extent i.e. auto flash mode, smile mode, etc.

2.2 Classification based on generation

1) First Generation Embedded System

First generation ES are designed with 8 bit microprocessor or 4 bit microcontroller. They have very simple hardware circuits. The firmwares are designed in assembly language. For eg: digital telephone keypad, stepper motor control, etc.

2) Second Generation Embedded System

Second generation ES are designed with 16 bit up or 8 bit μc. They have complex hardware configuration than first generation. They may contain embedded OS. Eg: DAS.

3) Third Generation Embedded System

Third generation ES are designed with 32 bit up or 16 bit μc. They consist of application specific IC. The concept of DSP emerges. Eg: Robotics.

4) Fourth Generation Embedded System

Fourth generation ES are designed with 64 bit up or 32 bit μc. They consist of system on chip and multi core processors with tight integration and miniaturization. Eg: smart phones.

1.3 Purpose of Embedded System

- 1) Data collection, storage and representation
- 2) Data communication
- 3) Data processing
- 4) Monitoring
- 5) Control
- 6) Application specific UI

1.4 Applications of ES

- 1) Consumer Electronics (camera, radio)
- 2) Home Appliances (TV, DVD player, washing machine)
- 3) Home Automation and security (CCTV, burglar alarm, fire alarm)
- 4) Industry Automation (Engine control)
- 5) Telecommunication (cell phones)
- 6) Networking (Routers, switch)
- 7) Computer peripherals (printer, fax)
- 8) Health science (ECG machine, disease identification system)
- 9) Biometrics (Finger print recognition, face detection)
- 10) Banking (ATM, currency counter)

1.5 Embedded System Design Metrics

- 1) Unit Cost (monetary cost of manufacturing each copy of system)
- 2) NRE Cost (one time monetary cost of designing system)
- 3) Size (Physical space in bytes or gates required)
- 4) Performance (Execution time of system)
- 5) Power (Amount of power consumed by the system)

- 6) Flexibility (ability to change functionality without incurring NRE cost)
- 7) Time to prototype (time needed to build working version)
- 8) Time to market (time required to develop a system upto release)
- 9) Maintainability (ability to modify system after initial release)
- 10) Correctness (correct functioning by the system)
- 11) Safety (Probability that system will not cause harm)

→ Design metrics are the measures of implementation features of a system

1.6 Embedded system Vs. General Purpose Computing System

- 1) ES consists of specific hardware, embedded OS.
GPCS consists of generic hardware, GPOS.
- 2) ES is designed to perform specific set of functions.
GPCS is designed to perform various functions.
- 3) OS in ES is mandatory but in GPCS it is compulsory.
- 4) Performance is key factor of GPCS.
- 5) Maximum power saving requirements for ES.
- 6) ES is time critical.
- 7) ES is deterministic.
- 8) Programs in GPCS are alterable by end users.

Q) How can we meet best optimization of ES?

There are many design metrics that impacts the embedded system design. The key challenge is that improving one metric leads to worsening of another. So, to meet best optimization, the designer must be comfortable with various implementation technologies and must be able to migrate from one technology to another. This ensure best implementation for a given system.

Q) Simplified Revenue Model

- It is used to investigate loss of revenue occurs due to delayed entry of a product in the market.
- It assumes peak of market occurs at halfway point (w) of a product life even for delayed entry.
- The revenue for an on-time market entry is area of Δ on time.
- The revenue for delayed entry is area of Δ delayed.

$$\therefore \text{Revenue loss} = A(\text{On time}) - A(\text{delayed})$$

$$\therefore \text{Percentage revenue loss} = \{A(\text{on time}) - A(\text{delayed})\}/A(\text{on time}) * 100\%$$

Let market rise angle be θ .

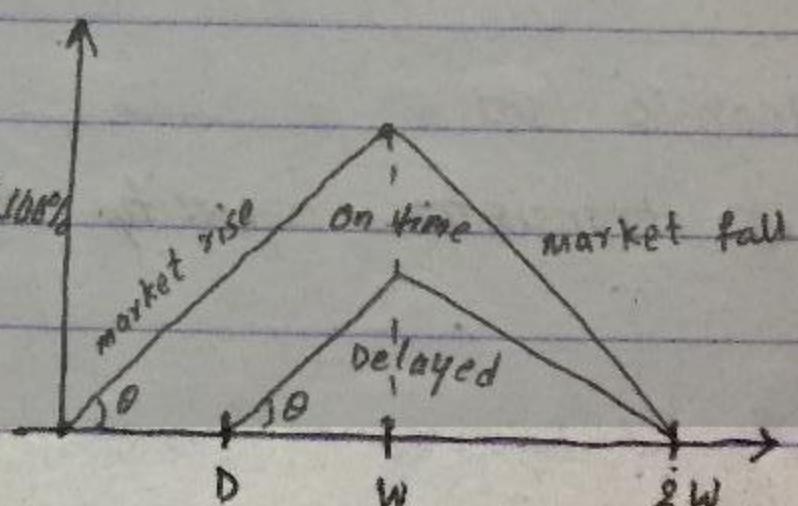
So,

$$A(\text{on time}) = 2 \left(\frac{1}{2} b \times h \right) = 2 \left(\frac{1}{2} \times w \times w \tan \theta \right) = w^2 \tan \theta$$

$$A(\text{delayed}) = \cancel{\frac{1}{2} (w-d) \times (w-d) \tan \theta} - \frac{1}{2} \times (2w-d) \times (w-d) \tan \theta$$

Now,

$$\begin{aligned} \text{Percentage revenue loss} &= [w^2 \tan \theta - \cancel{w^2 \tan \theta} + \cancel{\frac{1}{2} w d \tan \theta} - \cancel{\frac{1}{2} d^2 \tan \theta}] / w^2 \tan \theta * 100\% \\ &= \left[\frac{1}{2} (3wd - d^2) \right] \times 100\% \end{aligned}$$



Q) NRE and Unit Cost

→ total cost = NRE cost + unit cost * no. of units

$$\rightarrow \text{Per product cost} = \frac{\text{Total cost}}{\text{no. of units}}$$

Q) The design of disk drive has NRE cost \$100,000 and a unit cost \$20. How much will we have to add to cost of each product to cover NRE cost assuming sell of 100 units?

Ans →

$$\begin{aligned}\text{Added cost} &= \text{Amortized } \cancel{\text{NRE cost}} = \frac{\text{NRE cost}}{\text{no. of units}} \\ &= \frac{100\,000}{100} \\ &= \$1000\end{aligned}$$

Ans.

Q) Moore's law

IC transistor capacity doubles every 18 months.

2.1 Processor

Processor is a digital circuit that performs computational tasks. The minimum requirement to be a processor is the presence of controller and datapath.

The different processor technologies are as follows:-

1) General Purpose Processor (GPP):

It is a programmable circuit that can perform varieties of tasks. It consists of program memory and general data path. The datapath has large register array and one or more general purpose ALU.

2) Single Purpose Processor (SPP):

It is a digital circuit designed to perform exactly one program. Digital camera is a SPP. It only consists of data memory but not program memory.

3) Application Specific Processor (ASP)

It is a programmable circuit that is optimized for a particular class of applications. It consists of program memory, data memory, custom designed ALU and optimized datapath.

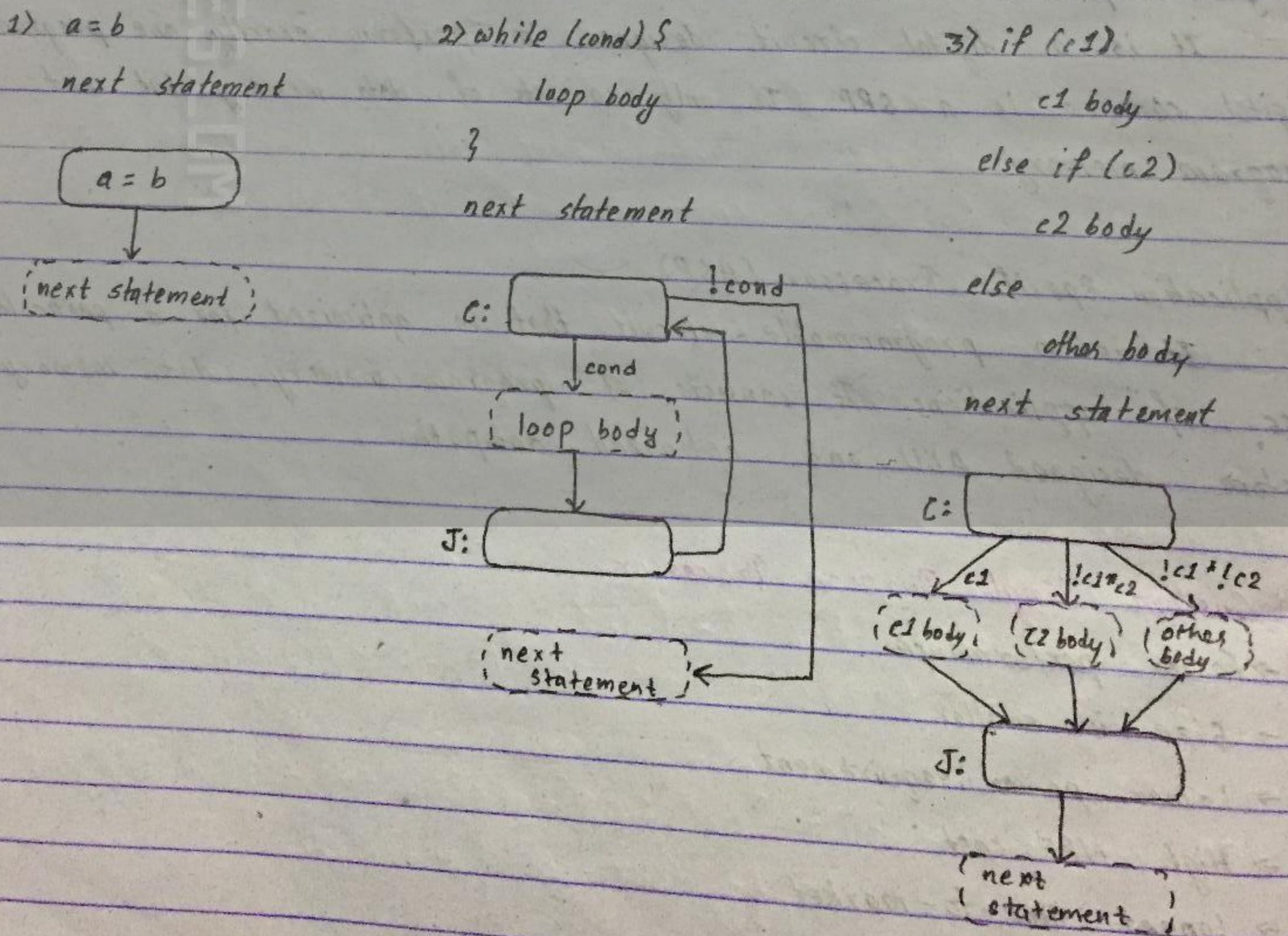
2.2 Custom Single Purpose Processor

- Faster performance
- Size is smaller
- Lower power requirement
- High NRE cost
- Longer time-to-market
- Less flexible

2.3 Designing custom single purpose processor

- 1) Develop an algorithm or function that computes the desired output.
- 2) Convert algorithm into a complex state diagram or FSMD (Finite State Machine with Data)
- 3) Divide functionality into datapath part and controller part.
datapath consists of interconnection of combinational and sequential components. Controller consists of pure FSM.
- 4) Complete controller design by implementing FSM with combinational logic.

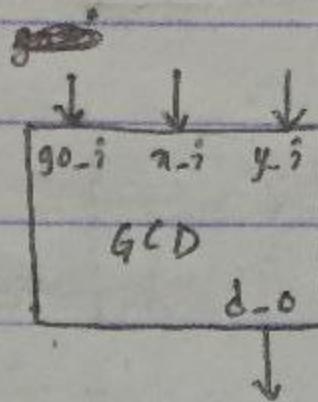
#FSMD Templates



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A) Greatest Common Divisor (GCD)

1) Black box diagram



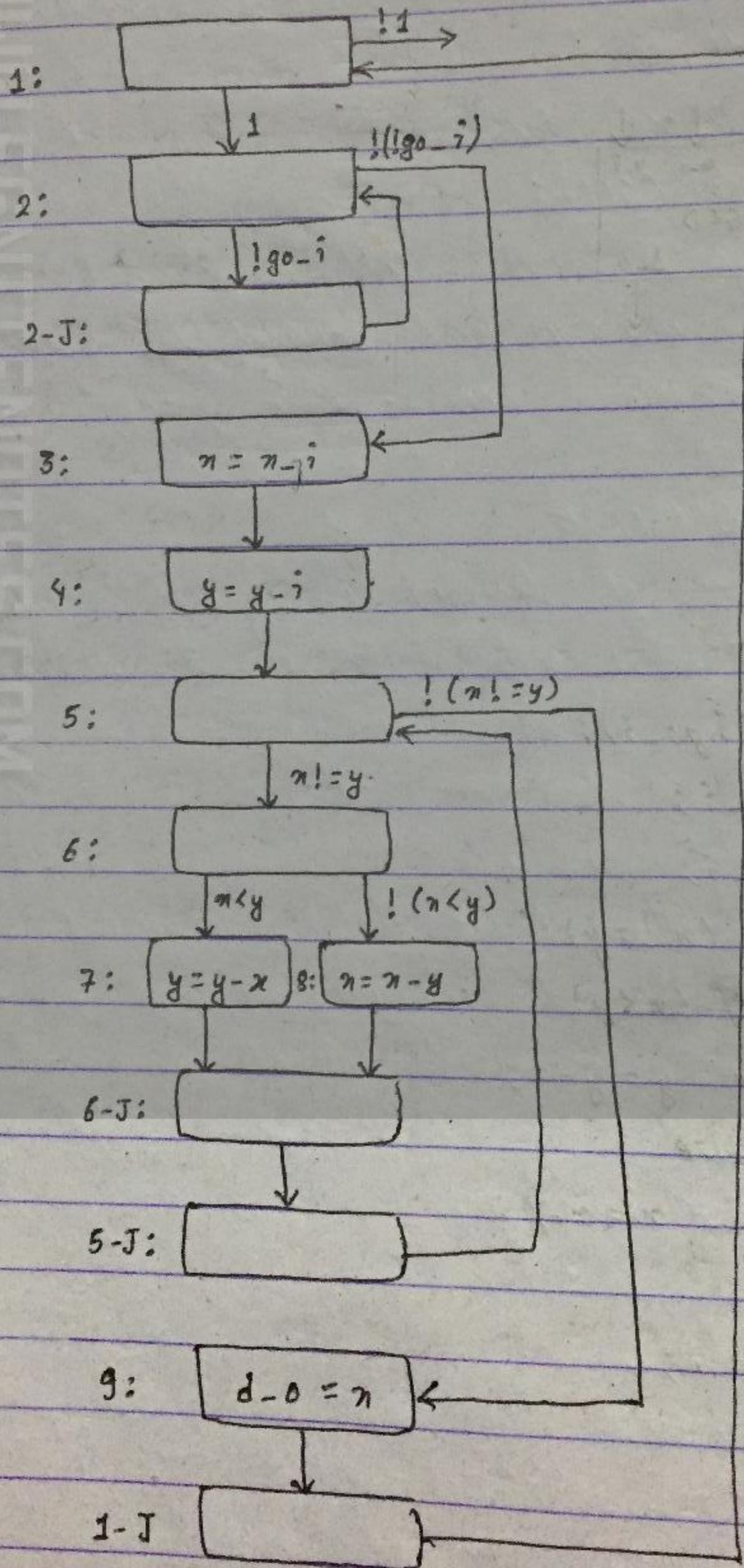
2) Algorithm

```

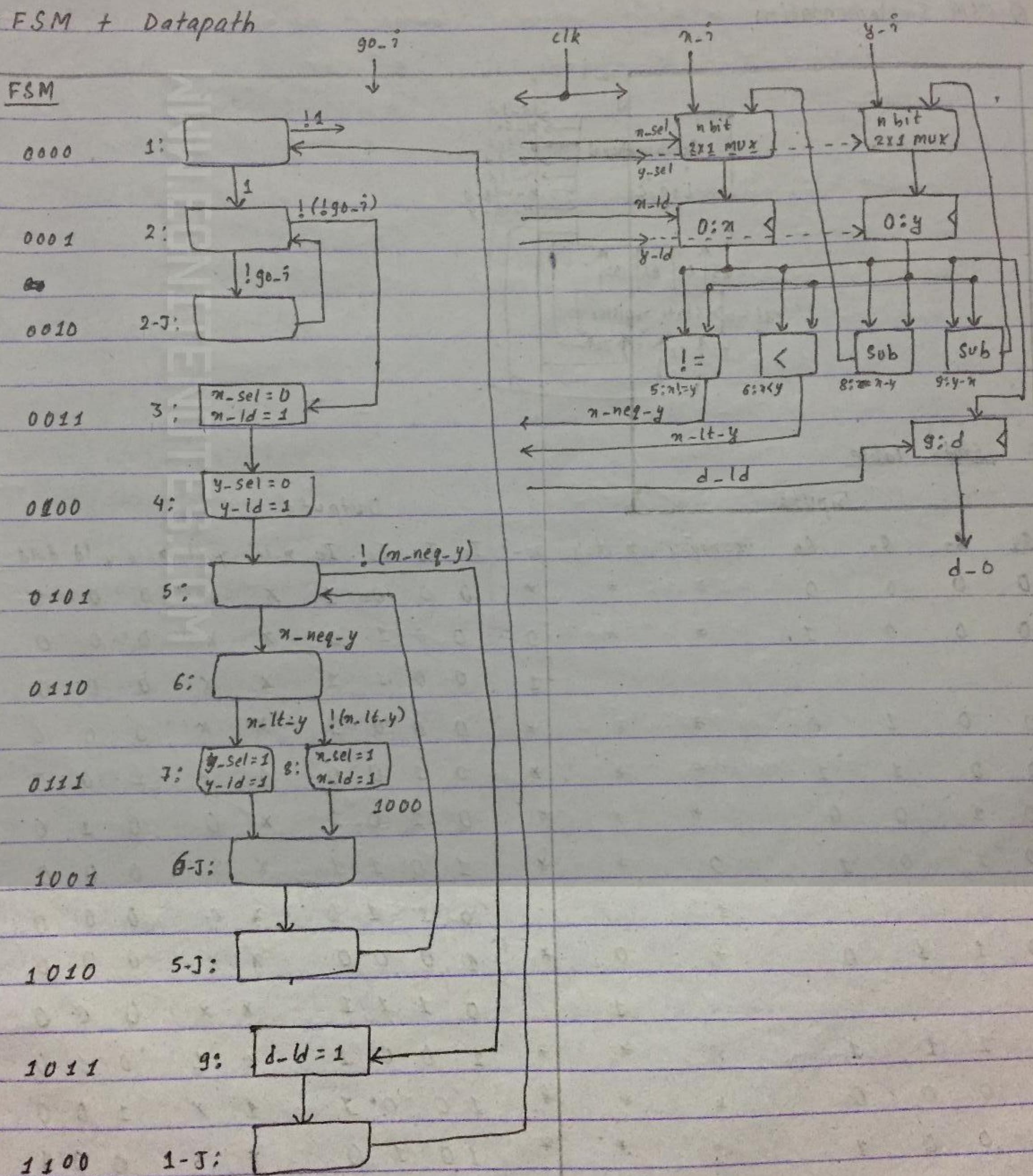
0: int n, y;
1: while (1) {
2:     while (!go-i);
3:     n = n-i;
4:     y = y-i;
5:     while (n != y) {
6:         if (n < y)
7:             y = y-n;
8:         else
9:             n = n-y;
}
  
```

The algorithm is a step-by-step pseudocode for the Euclidean algorithm. It starts with two integer variables, n and y. A loop begins with a condition that always evaluates to true (line 1). Inside this loop, another loop runs as long as n is not equal to y (line 5). If n is less than y (line 6), it subtracts n from y (line 7). Otherwise, it subtracts y from n (line 8). This process repeats until n equals y, at which point the loop exits.

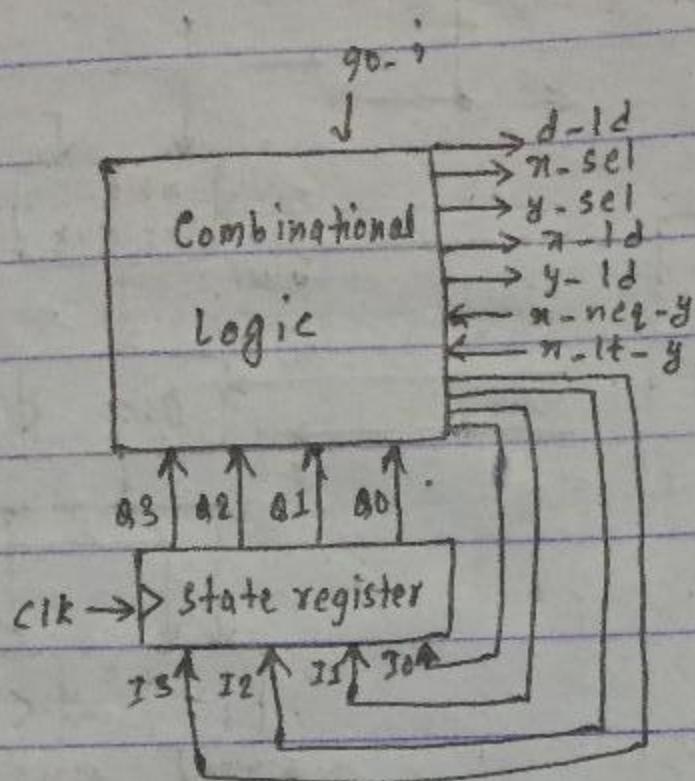
3) State Diagram or FSMD



4) FSM + Datapath



5) FSM Implementation



State Table

Inputs							Outputs								
B_3	B_2	B_1	B_0	$n\text{-neq-}y$	$n\text{-lt-}y$	$g_0\text{-}?$	I_3	I_2	I_1	I_0	$n\text{-sel}$	$y\text{-sel}$	$n\text{-ld}$	$y\text{-ld}$	$d\text{-ld}$
0	0	0	0	*	*	*	0	0	0	1	x	x	0	0	0
0	0	0	1	*	*	0	0	0	1	0	x	x	0	0	0
						1	0	0	1	1	x	x	0	0	0
0	0	1	0	*	*	*	0	0	0	1	x	x	0	0	0
0	0	1	1	*	*	*	0	1	0	0	0	x	1	0	0
0	1	0	0	*	*	*	0	1	0	1	x	0	0	1	0
0	1	0	1	0	*	*	1	0	1	1	x	x	0	0	0
				1			0	1	1	0	x	x	0	0	0
0	1	1	0	*	0	*	1	0	0	0	x	x	0	0	0
0	1	1	1	*	*	*	0	1	1	1	x	x	0	0	0
1	0	0	0	*	*	*	1	0	0	1	x	1	0	1	0
1	0	0	1	*	*	*	1	0	0	1	1	x	1	0	0
1	0	1	0	*	*	*	1	0	1	0	x	x	0	0	0
1	0	1	1	*	*	*	0	1	0	1	x	x	0	0	0
1	1	x	x	*	*	*	1	1	0	0	x	x	0	0	0
1	1	x	x	*	*	*	0	0	0	0	x	x	0	0	0

a) Lowest Common Multiple (LCM)

$$\rightarrow \text{LCM} = \frac{\cancel{\text{GCD}}}{\cancel{a \times b}} \frac{a \times b}{\text{GCD}}$$

Algorithm

```

0: int x, y, z;
1: while (1) {
2:   while (!go - i);
3:   n = x - i;
4:   y = y - i;
5:   z = n * y;
6:   while (n != y) {
7:     if (n < y)
8:       y = y - n;
else
9:   n = n - y;
}
10:  d - o = z / n;
}

```

a) Fibonacci number up to 'n' places

1, 1, 2, 3, 5, 8, 13, 21, , n^{th} place

Algorithm

```
int n1, n2, temp, count, n;
```

```
while (1) {
```

```
    while (!go - i);
```

```
    n1 = 1;
```

```
    n2 = 1;
```

```
    n = n - i;
```

```
    count = 0;
```

```
    while (count < n) {
```

```
        if (count != 0 && count != 1) {
```

```
            temp = n1;
```

```
            n1 = n2;
```

```
            n2 = n1 + temp;
```

}

```
        fib - 0 = n2;
```

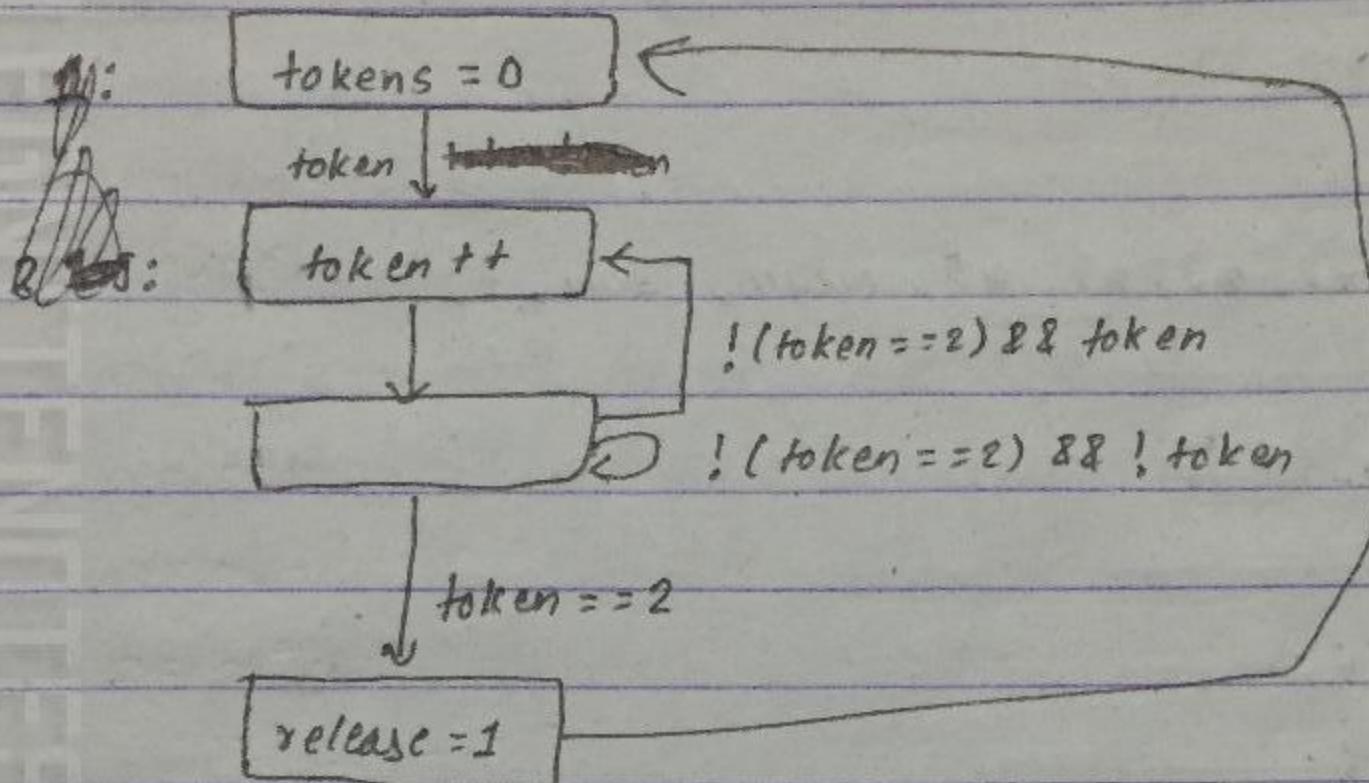
```
        count ++;
```

}

}

15:

Q) A subway has ES controlling turnstile, which releases when two tokens are deposited. Draw FMD.



Q) Factorial and check if prime

```
int n, f, temp, i  
while (1) {  
    while (!go_i);  
    i = 2;  
    n = n - i;  
    temp = n;  
    f = 1;
```

```
    while (temp != 0) {
```

```
        f = f * temp;
```

```
        temp --;
```

```
}
```

```
f - o = f;
```

~~```
#(f - o)
```~~

```
while (i < n) {
```

```
 if (n % i == 0)
```

```
 p - o = 0;
```

```
 else
```

```
 p - o = 1;
```

a) Median and variance of 5 numbers entered by user

Median = Value of  $(\frac{n+1}{2})^{\text{th}}$  item

Variance =  $\frac{\sum (x - \mu)^2}{N}$

int n, n1, n2, n3, n4, n5, mean, sum, i;

while (1) {

    while (!go-i);

    n = 5;

    n1 = n1 - i;

    n2 = n2 - i;

    n3 = n3 - i;

    n4 = n4 - i;

    n5 = n5 - i;

    mean = (n1 + n2 + n3 + n4 + n5) / 5;

    median - 0 = n  $\lceil \frac{n+1}{2} \rceil$ ;

    sum = 0;

    i = 0;

    while (i < 5) {

        sum = sum + (n[i] - mean) \* (n[i] - mean);

        i++;

}

    variance - 0 = sum / n;

}

## 2.4 Optimization

Optimization is the technique of improving the design metrics so as to get the best possible values of various design metrics.

The optimization opportunities in custom SPP are as follows :-

### 1) Optimizing original program:

The algorithms are analyzed in terms of time complexity and space complexity, and hence we try to develop more efficient alternative algorithms. It involves decreasing of no. of computations and size of variables if possible.

#### Eg: Optimized GCD program

```

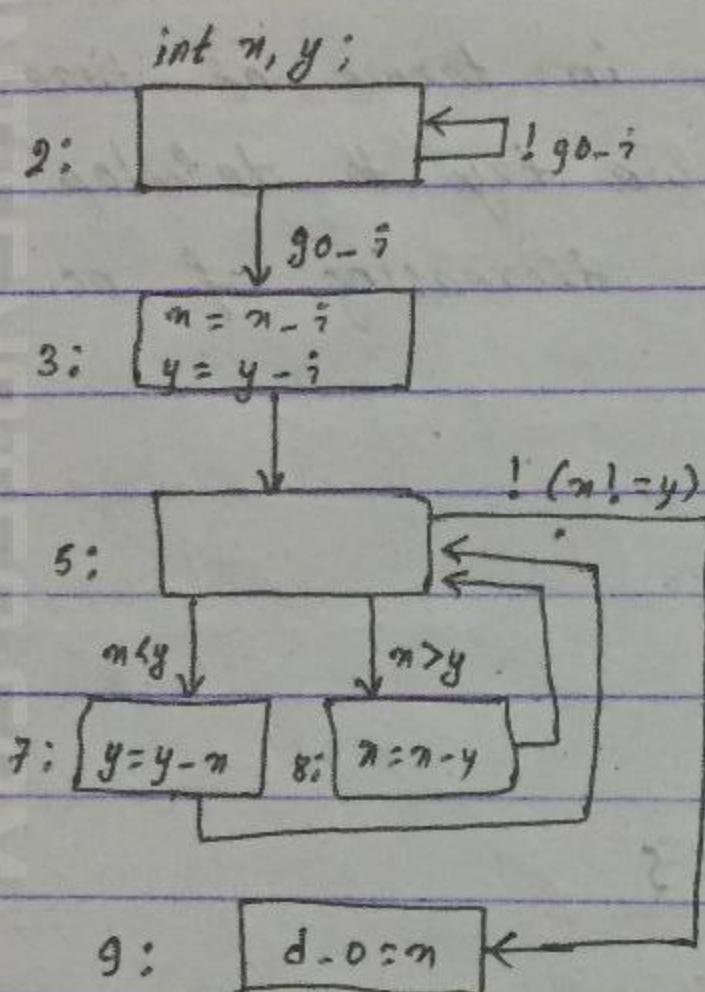
int n, y, r;
while (1) {
 while (!go-i);
 if (n-i >= y-i) {
 n = n-i;
 y = y-i;
 } else {
 n = y-i;
 y = n-i;
 }
 while (y != 0) {
 r = n % y;
 n = y;
 y = r;
 }
 d = 0 = n;
}

```

### 2) Optimizing FSMD

The states that can be merged are merged to reduce the number of states. The design must be aware of whether o/p timing may or may not be modified.

Eg: Optimized GCD FSMD



### 3) Optimizing Datapath

Many functional operations can share a single functional unit if those operations occur in different stages.

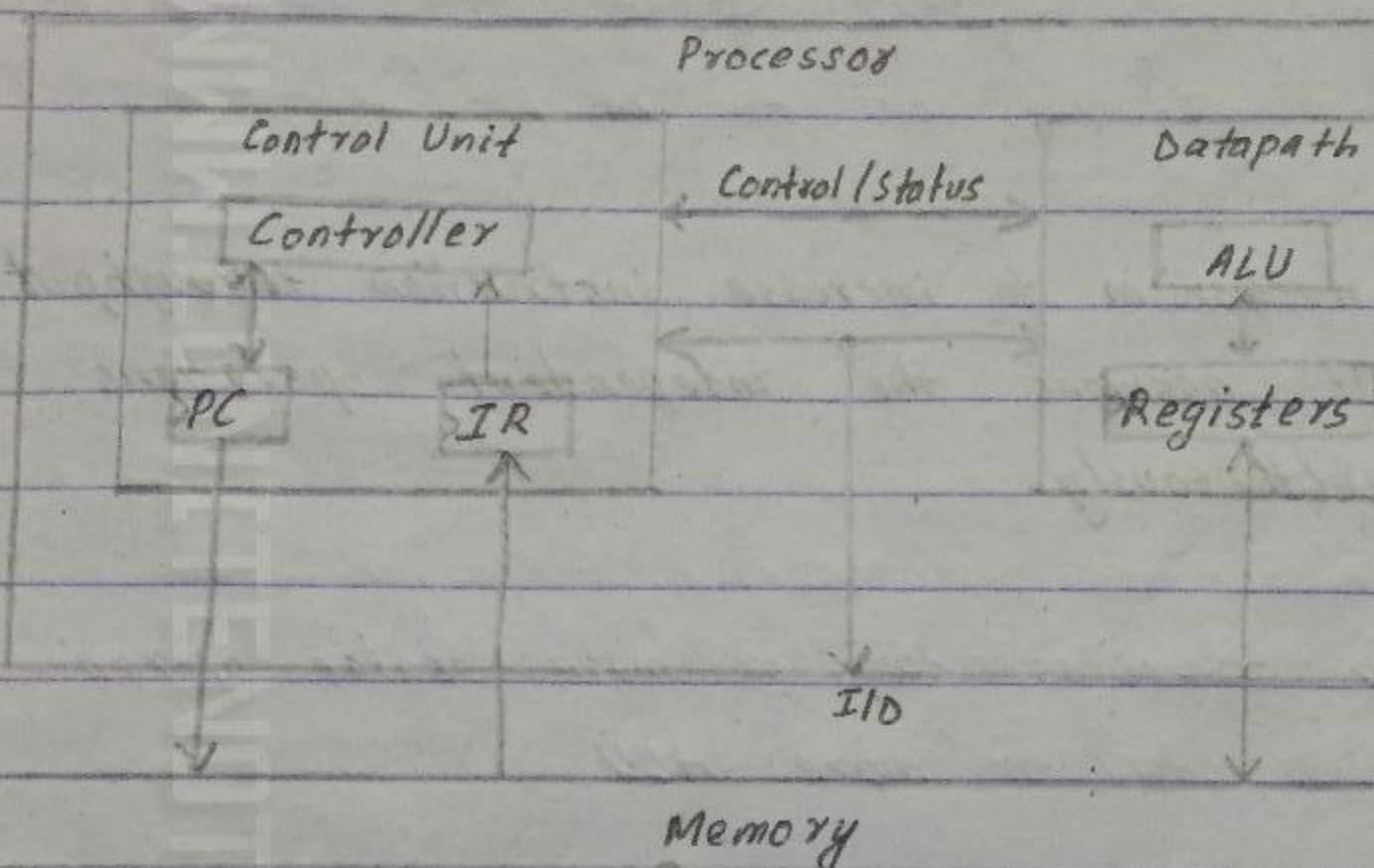
Eg: In GCD datapath, single subtractor can be used and selection can be done using multiplexor.

#### 4) Optimizing FSM

FSM can be optimized using state encoding and state minimization. State encoding is the task of assigning a unique bit pattern to each state in an FSM. We can use more than  $\log_2(n)$  bits to encode  $n$  states.

State minimization is the task of merging equivalent states into a single state.

## 3.1 Basic Architecture



- It consists of general datapath.
- Control unit does not store algorithm.
- Algorithm is programmed into memory.

## 3.2 Operations

- 1) **Fetch Instruction:** It gets the next instruction as indicated by location in memory pointed by PC and stores into IR.
- 2) **Decode Instruction:** It determines the actual operations performed by the instruction in IR.
- 3) **Fetch Operands:** It gets the operand data needed for instruction from memory to appropriate registers of datapath.
- 4) **Execute:** The actual arithmetic or logical operations is performed by moving data through ALU.

5) Store Results: It writes the data from datapath register into the memory.

### # Pipelining

Pipelining is the mechanism to increase instruction throughput of a microprocessor. It assumes the independent operations to be performed simultaneously.

→ Superscalar microprocessor executes two or more scalar operations in parallel and requires two or more ALU.

→ VLIW (Very Long Instruction Word) architecture is a static superscalar microprocessor that encodes several operations in a single machine instruction.

### 3.3 Programmer's View

Programmer does not need detailed understanding of architecture. They just need to know which instructions can be executed. Generally, there are two levels of instructions: assembly level and structured languages.

→ Instruction set is the legal set of instructions that can be processed by a processor.

→ Addressing modes indicates how the data for any operation is referenced in the instruction.

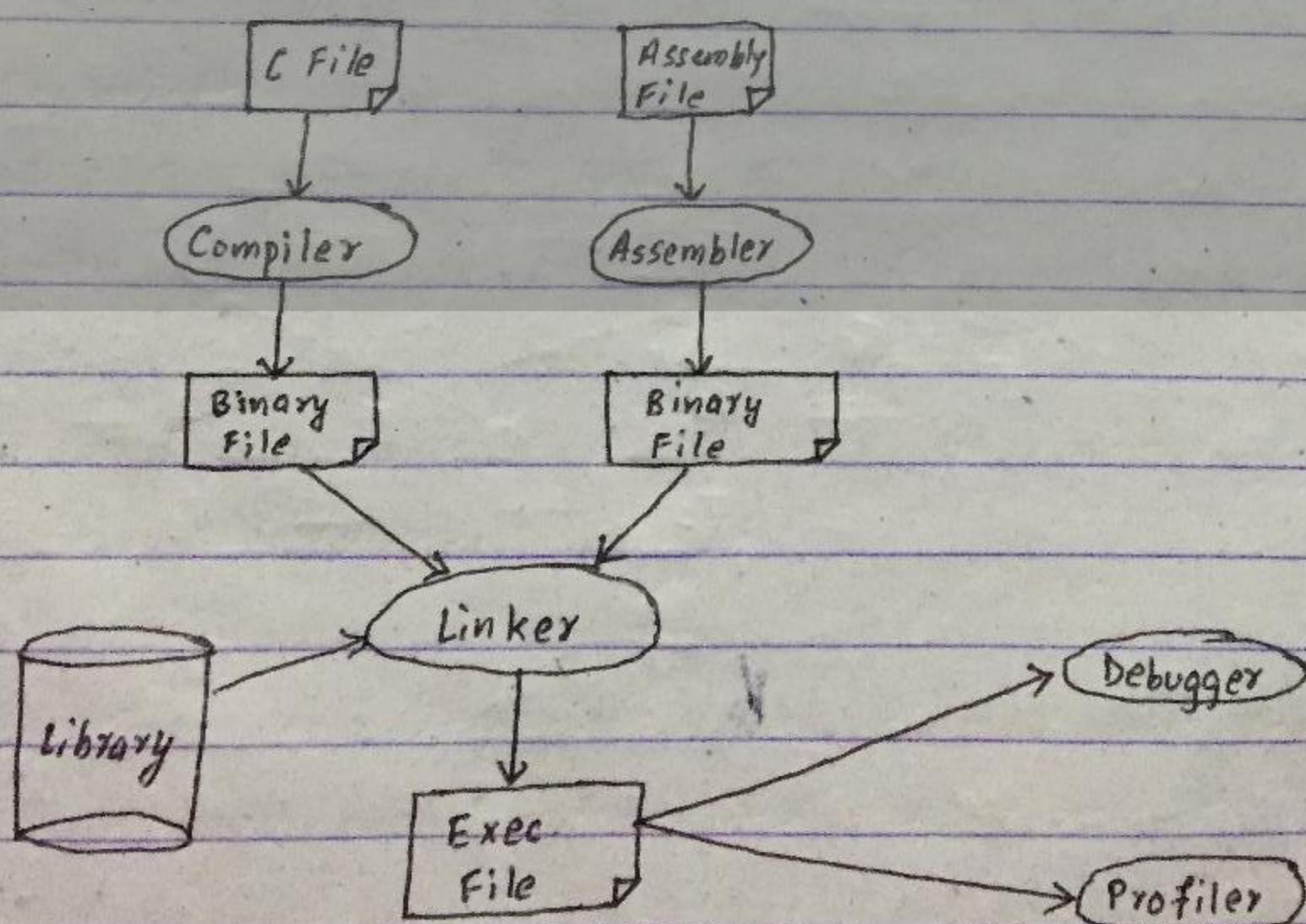
### 3.4 Programmer's Considerations

- 1> Program and data memory space
- 2> Registers
- 3> I/O
- 4> Interrupts
- 5> Operating System

### 3.5 Development Environment

- Development processor : Processor on which programs are written.
- Target processor : Processor that will run the program.
- If development and target processor are different, the code can be run by downloading to target processor or by simulation.
- Simulation can be done using HDL and Instruction Set Simulator (ISS)

### 3.6 Software Development Process



### 3.7 Application Specific Instruction- Set Processor (ASIP)

ASIP is the processor targeted for a particular domain. The architecture is domain specific but can be programmed. Eg: microcontroller, Digital Signal Processor

### 3.8 Selection of microprocessor

- 1) Speed (Clock speed or instructions per second)
- 2) Power requirements
- 3) Size (Program and data memory space)
- 4) Cost
- 5) Development environment
- 6) Technical support
- 7) Experience

## Chapter 4

### Memory

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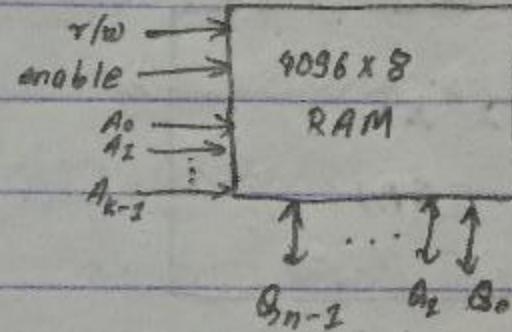
#### 4.1 Memory basics

- $m \times n$  memory stores  $m$  words of  $n$  bits each.
- $m = 2^k$ , where  $k$  = no. of address input signals.
- $n$  indicates no. of data signals.
- $r/w$  selects read or write
- enable : read or write only when asserted.

Consider a memory with  $4096 \times 8$ .

$$\rightarrow k = 12$$

$$\rightarrow n = 8$$



#### 4.2 Memory write ability and Storage permanence

##### → Write Ability

Write ability is the manner and speed that a particular memory can be written. The ranges of write ability are:-

- 1) High end (processor writes to memory quickly → RAM)
- 2) Middle range (processor writes to memory slowly → FLASH, EEPROM)
- 3) Lower range (special equipment used to write to memory → EPRDM, OTP ROM)
- 4) Low end (bits stored only during fabrication → Masked ROM)

##### → Storage Permanence

Storage permanence is the ability of memory to hold its stored bits after they have been written. The ranges are:-

- 1) High end (never loss bits) → Masked ROM
- 2) Middle range (holds bit for days or years after power cut off → NVRAM)

- 3) Lower range (holds bits as long as power is supplied  $\rightarrow$  SRAM)  
 4) Low end (lose bits immediately after written  $\rightarrow$  DRAM)

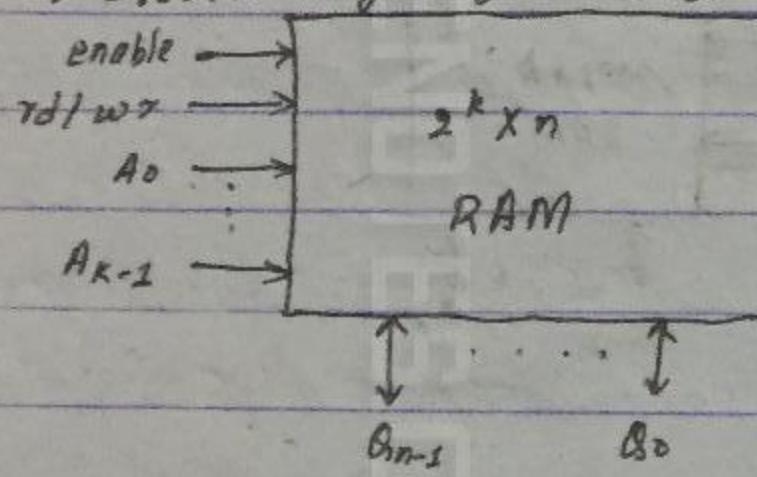
### 4.3 Types of Memory

#### 1) Random Access Memory (RAM)

$\rightarrow$  It can be read and written easily.

$\rightarrow$  It is volatile memory.

$\rightarrow$  Electrically byte level erasing     $\rightarrow$  Electrically write



#### $\rightarrow$ SRAM

$\rightarrow$  Bits are stored as on/off switches.

$\rightarrow$  Charges are not leaked.

$\rightarrow$  Refreshing is not needed.

$\rightarrow$  No refresh circuits

$\rightarrow$  Larger per bit

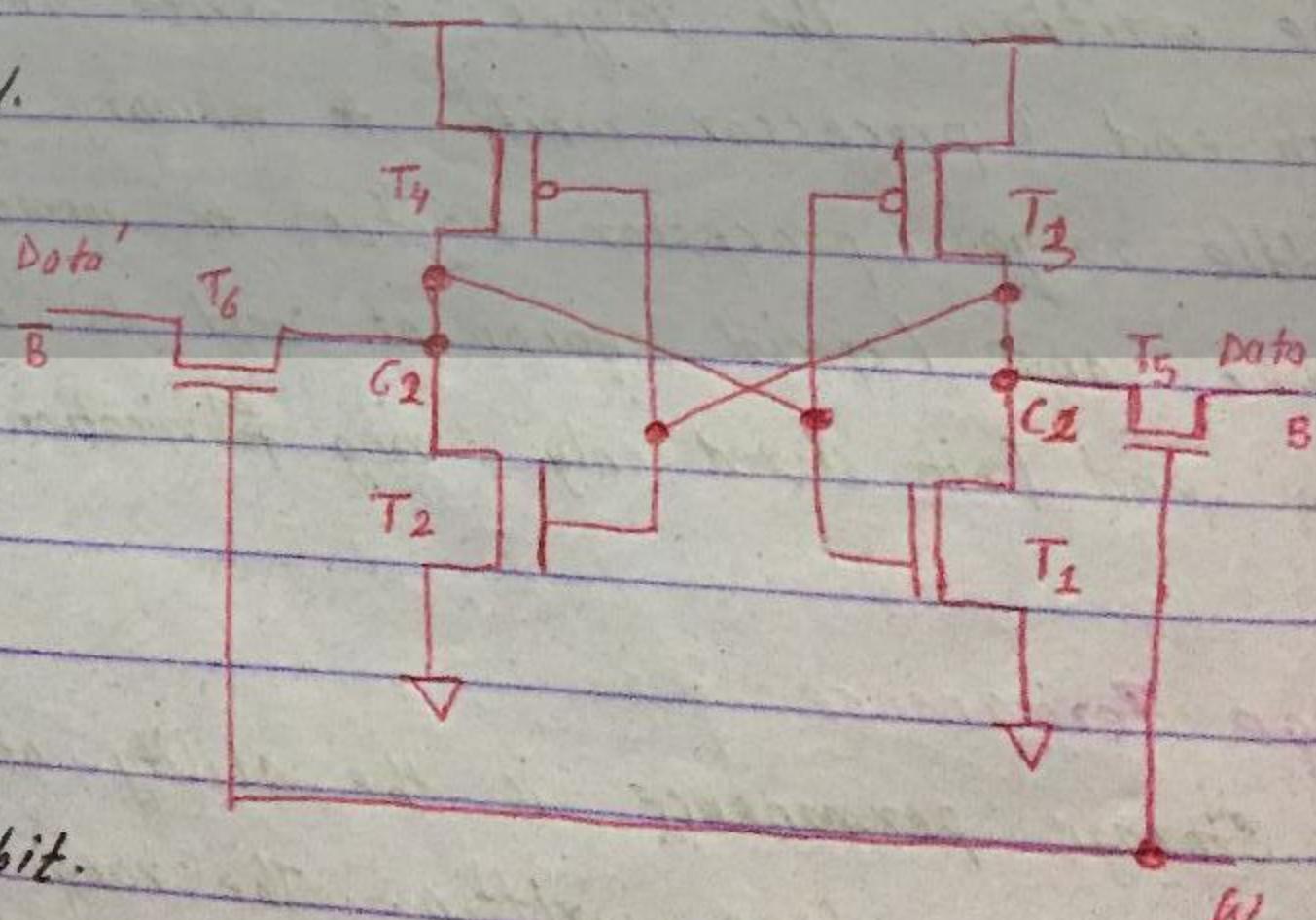
$\rightarrow$  Complex construction

$\rightarrow$  Expensive

$\rightarrow$  Faster

$\rightarrow$  Cache

$\rightarrow$  Uses flip flops to store bit.



→ In state 1;

$C_1 = \text{high}$ ,  $C_2 = \text{low}$

$T_2 T_3$  on

→ In state 0;

$C_1 = \text{low}$ ,  $C_2 = \text{high}$

$T_1 T_4$  on

→ Write : apply value to B and  $\bar{B}$

→ Read : value is on B

### → DRAM

→ Bits are stored as charge in capacitor

→ Charges leak

→ Need refreshing

→ Have refresh circuits

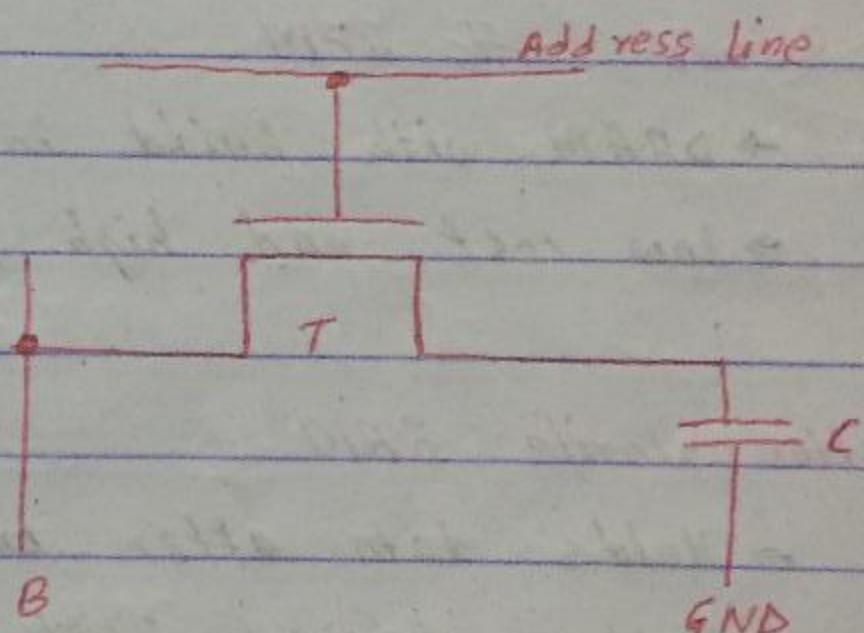
→ Cheaper

→ Slower

→ Smaller per bit

→ Main memory

→ Level of charge determines value



→ When address line is active, transistor switch closes, so bit is read or written

→ During write operation, transfers charge to capacitor.

→ During read operation, address line selected and charge from capacitor fed via B to sense amplifier.

### → Enhanced DRAM

- Enhanced DRAM are built around conventional DRAM core.
- It is a DRAM that includes small amount of static RAM so as to access memory faster.
- First, data is checked in SRAM
- If miss, data is accessed from DRAM.
- Fast page mode DRAM : access row contents [RAS, CAS, CAS, CAS]
- Extended data out DRAM : EPM with closely spaced CAS.
- Synchronous DRAM : Driven with rising clock edge
- Double data rate SDRAM : SDRAM with both clock edges.

### → Pseudo static RAM

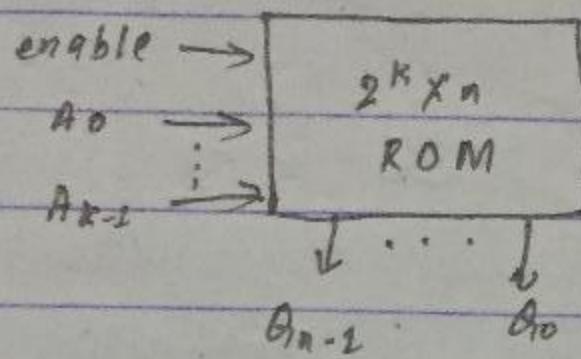
- DRAM with build in memory refresh controller
- low cost and high density

### → Non volatile RAM

- Holds data after external power removed
- Battery backed RAM
- SRAM with EEPROM

## 2) Read Only Memory (ROM)

→ Non-volatile memory



### → Masked ROM

→ Programmed during fabrication by creating masks.

→ Low write ability

→ High storage permanence

### → OTP ROM

→ External equipment is needed to write.

→ Electrically write mechanism

### → EEPROM

→ Electrically write

→ Erase using UV light (chip level)

### → EEPROM

→ Byte level electrically erasing

→ Electrical write

### → Flash memory

→ Block level electrically erasing

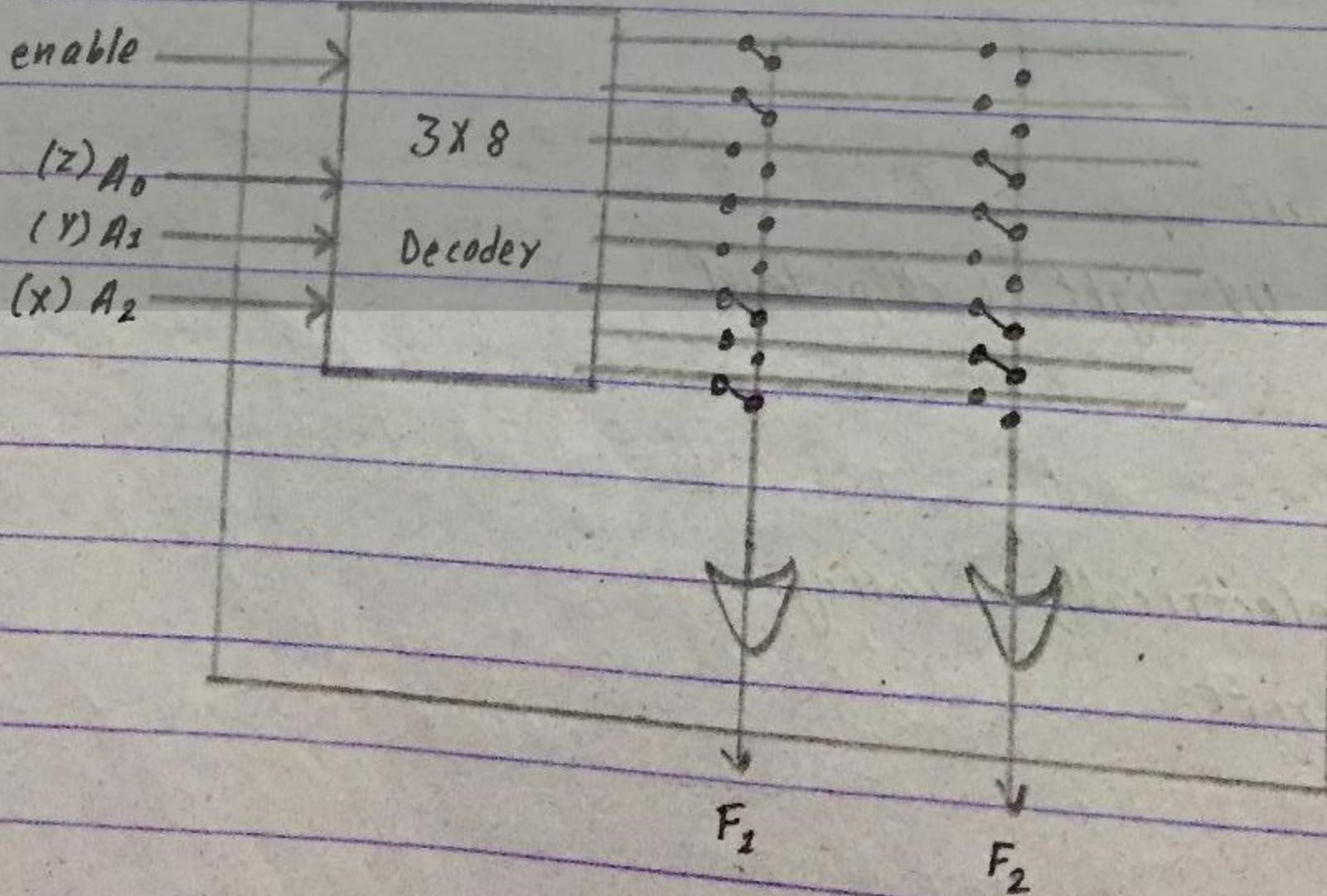
## 9.9 Composing memory

→ Design  $8 \times 2$  ROM with:

| <u>x</u> | <u>y</u> | <u>z</u> | <u><math>F_1</math></u> | <u><math>F_2</math></u> |
|----------|----------|----------|-------------------------|-------------------------|
| 0        | 0        | 0        | 1                       | 0                       |
| 0        | 0        | 1        | 1                       | 0                       |
| 0        | 1        | 0        | 0                       | 1                       |
| 0        | 1        | 1        | 0                       | 1                       |
| 1        | 0        | 0        | 0                       | 0                       |
| 1        | 0        | 1        | 1                       | 1                       |
| 1        | 1        | 0        | 0                       | 1                       |
| 1        | 1        | 1        | 1                       | 0                       |

Ans →

8 × 2 ROM



→ Compose  $1K \times 8$  ROMs into  $2K \times 16$  ROM.

Ans →

$1K \times 8$  ROM

$k = 10$

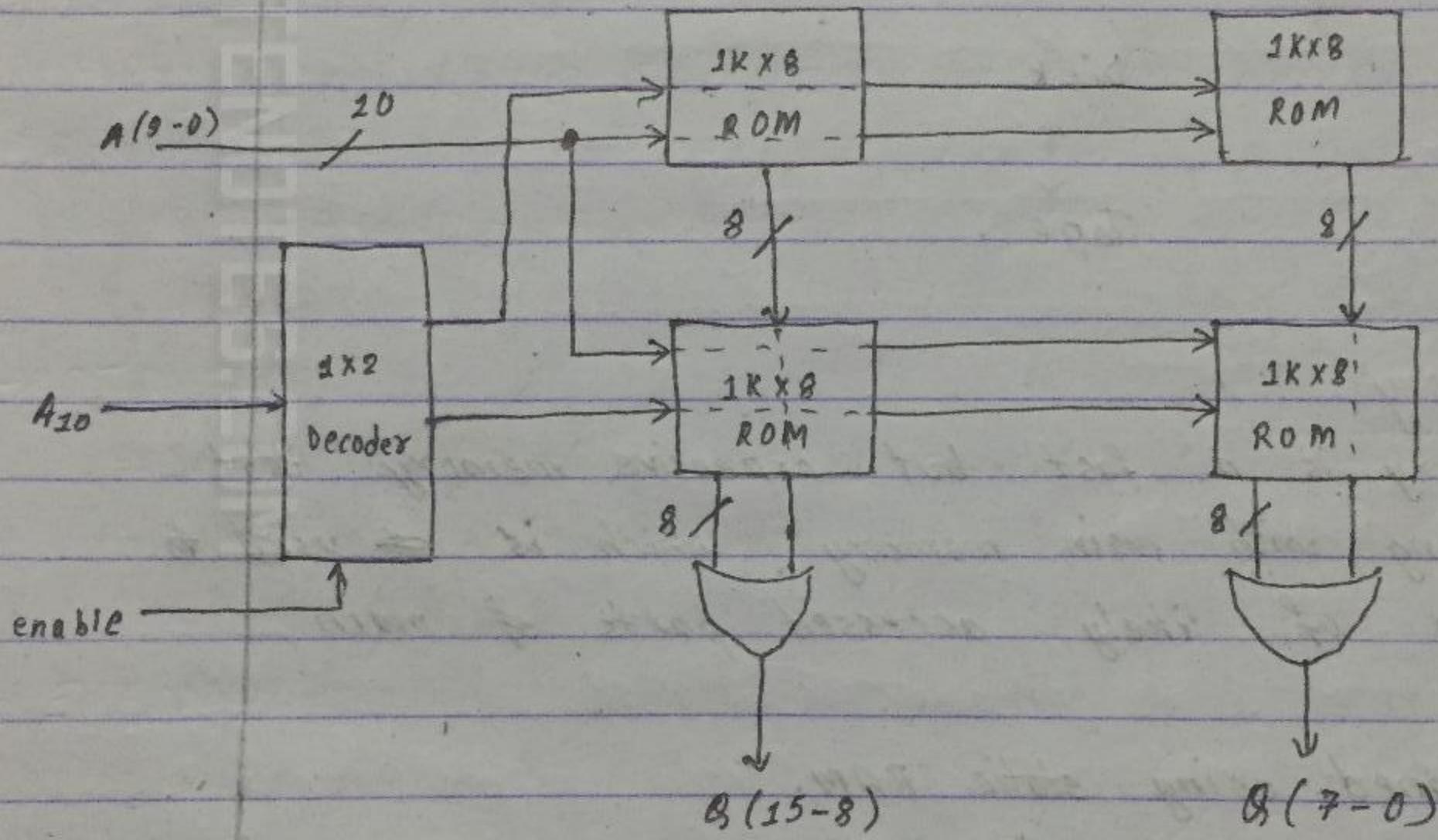
$n = 8$

$2K \times 16$  ROM

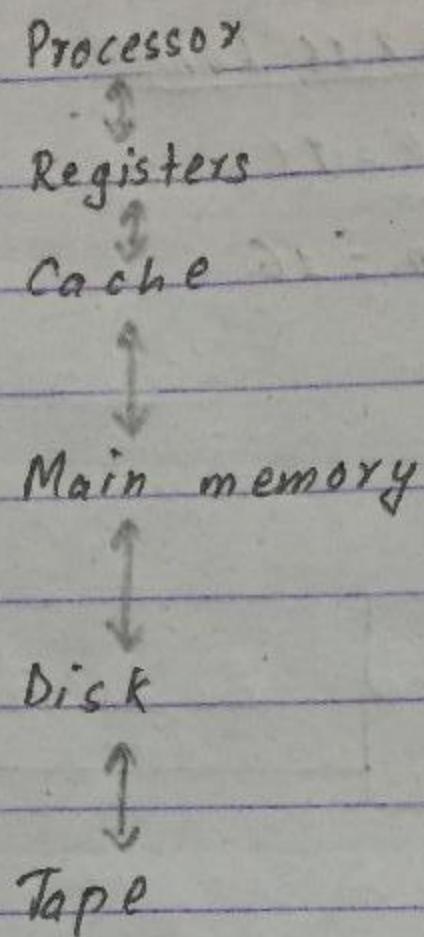
$k = 11$

$n = 16$

$2K \times 16$  ROM



## 4.5 Memory Hierarchy



## 4.6 Cache Memory

- Cache memory is a fast but expensive memory that is used along with main memory which is ~~not~~ used to store copies of likely accessed parts of main memory.
- It is designed using static RAM.
- When there is request for main memory access, firstly copy in cache is checked. If cache hit, memory access becomes quick. If cache miss, read from the main memory.

### → Cache Mapping

- 1) Direct mapping
- 2) Fully associative mapping
- 3) Set associative mapping

### → Cache Replacement

- Choosing which cache block to replace.
- Random replacement
- Least recently used (LRU) policy
- First in first out (FIFO) policy

### → Cache Write Techniques

- Updating the main memory
- Write-through (Write to main memory whenever cache is written)
- Write-back (Write to main memory only when cache block is being replaced)

### → Cache Impacts

|                     | <u>2K cache</u> | <u>4K cache</u> | <u>8K cache</u> |
|---------------------|-----------------|-----------------|-----------------|
| miss rate           | 15%             | 6.5%            | 5.565%          |
| hit <del>cost</del> | 2 cycle         | 3 cycle         | 4 cycle         |
| miss cost           | 20 cycle        | 20 cycle        | 20 cycle        |

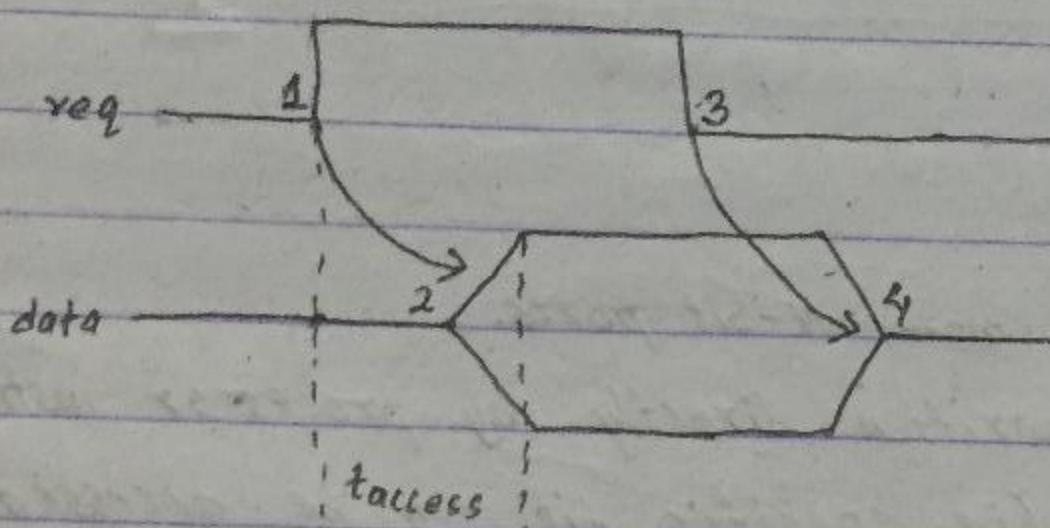
av. cost of memory access = (hit rate \* hit cost) + (miss rate \* miss cost) cycles

### 5.1 Communication Basics

- Bus is a set of wires with a single function within a communication.
- Protocol describes the rules for communicating within a bus.
- Each sub protocol is called transaction or bus cycle.
- Actor ~~are~~ is a processor or memory involved in data transfer.
- Data direction indicates direction of transferred data.
- Address indicate where data should go to or come from.
- Control methods are schemes for initiating and ending the transfer.

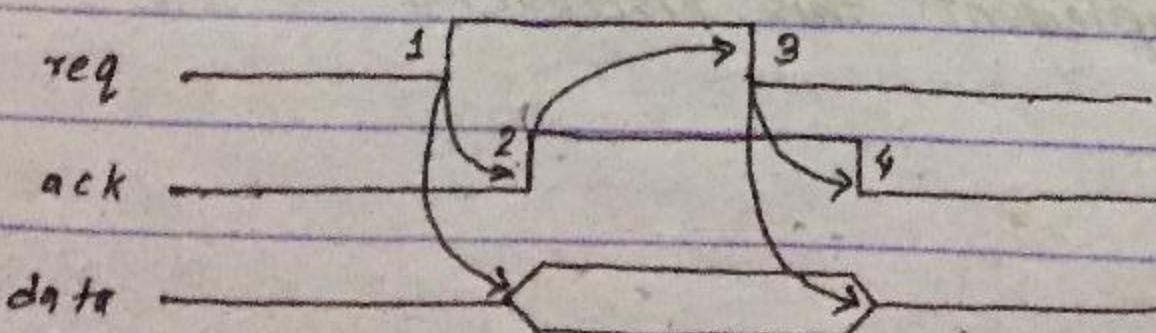
### → Strobe Protocol

- The master uses one control line (request line) to initiate data transfer.
- The transfer is considered to complete after some fixed time.

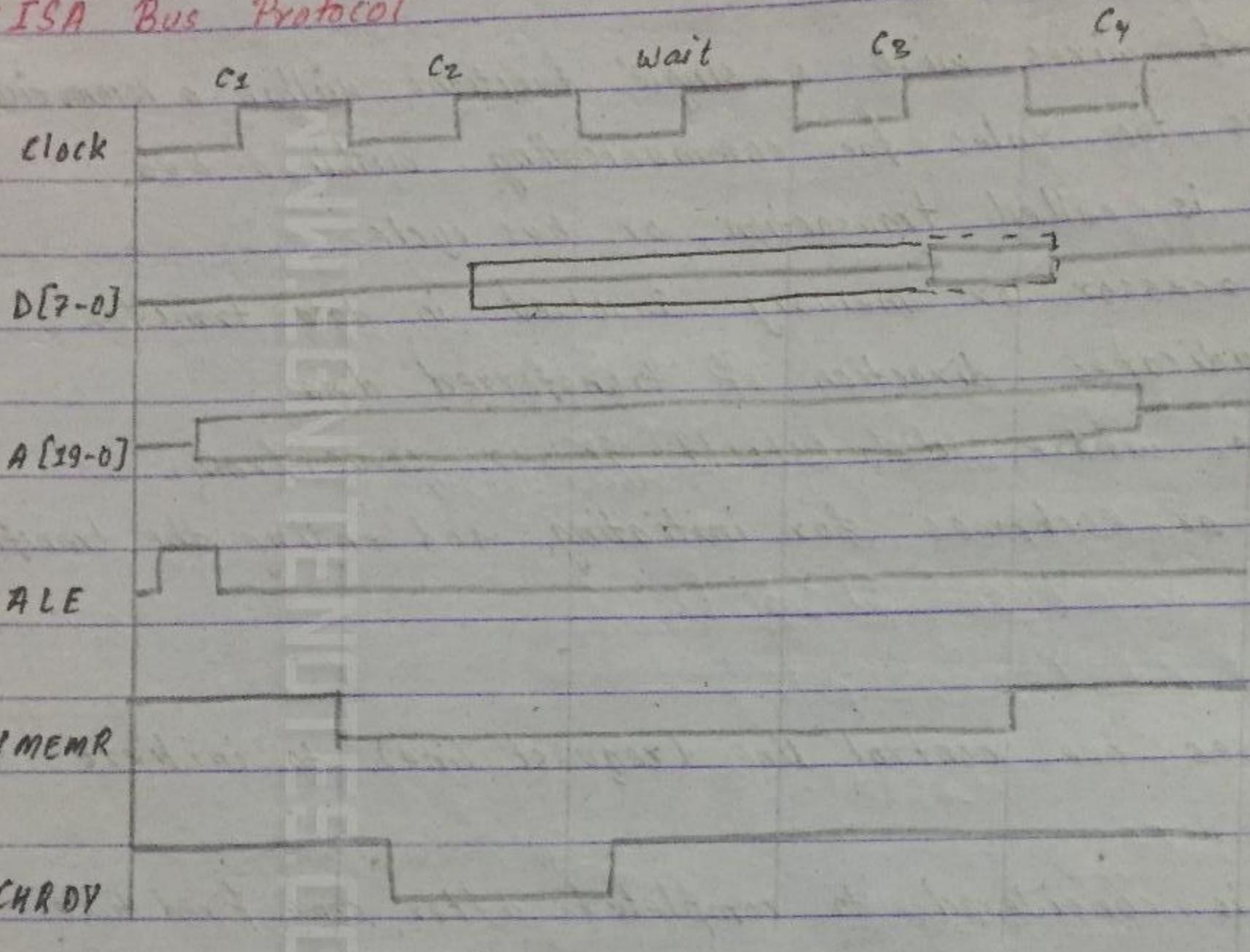


### → Handshake Protocol

- Master uses request line to initiate transfer.
- The servant uses acknowledge line to inform master when data is ready.



→ ISA Bus Protocol



## 5.2 Port and Bus Based I/O

→ Port based I/O

- Processor contains one or more N-bit ports.
- A port can be read or written directly by processor instruction.
- Port are bit addressable (i.e. specific bit can be accessed)

→ Bus based I/O

- Memory is accessed using bus lines.
- Bus protocol is built within microprocessor
- A software does not implement this protocol.

→ Memory mapped I/O and Standard I/O

→ Peripherals occupy specific addresses in existing address space.

In standard I/O, bus includes M/I/O to indicate whether the access is to memory or to a peripheral.

→ In memory mapped, no special instructions are needed to communicate with peripherals.

→ In standard I/O, memory address is not lost.

### 5.3 Interrupts

→ Using fixed ISR location

1) μP is executing the main program.

2) Peripheral (P1) receives ilp data and asserts Int to request service.

3) After completing current instruction, μP sees int. It saves PC and set PC to ISR fixed location.

4) The ISR reads data and perform necessary functions. After P1 is read, P1 deasserts Int.

5) The ISR returns and then PC is restored.

→ Using vectored interrupt

→ When μP sees int, it saves PC and asserts Inta

→ P1 detects Inta and puts interrupt address vector on data bus.

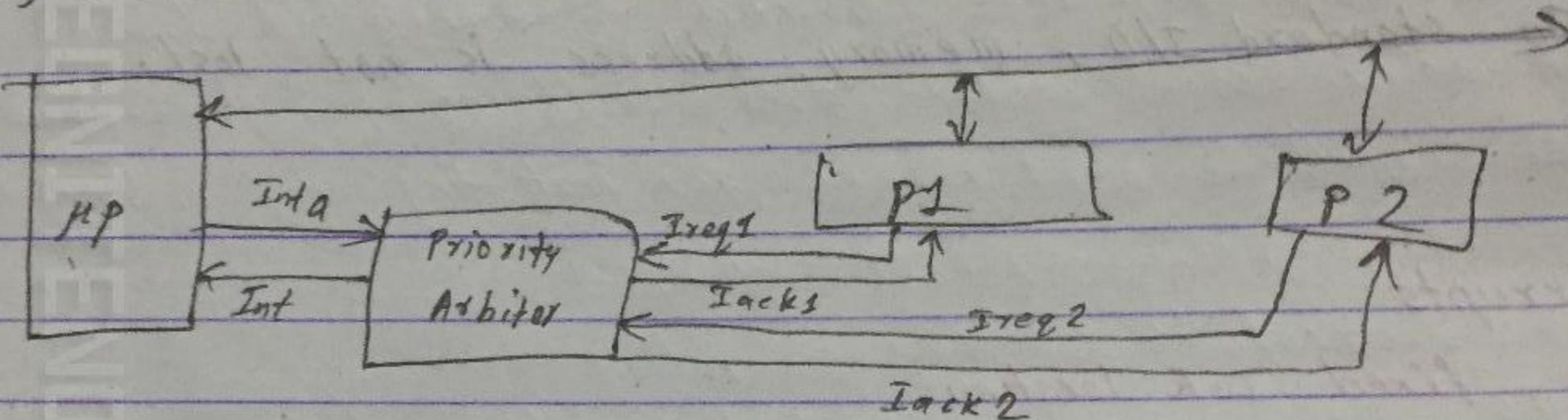
→ μP jumps to address on the bus.

### 5.4 Direct Memory Access (DMA)

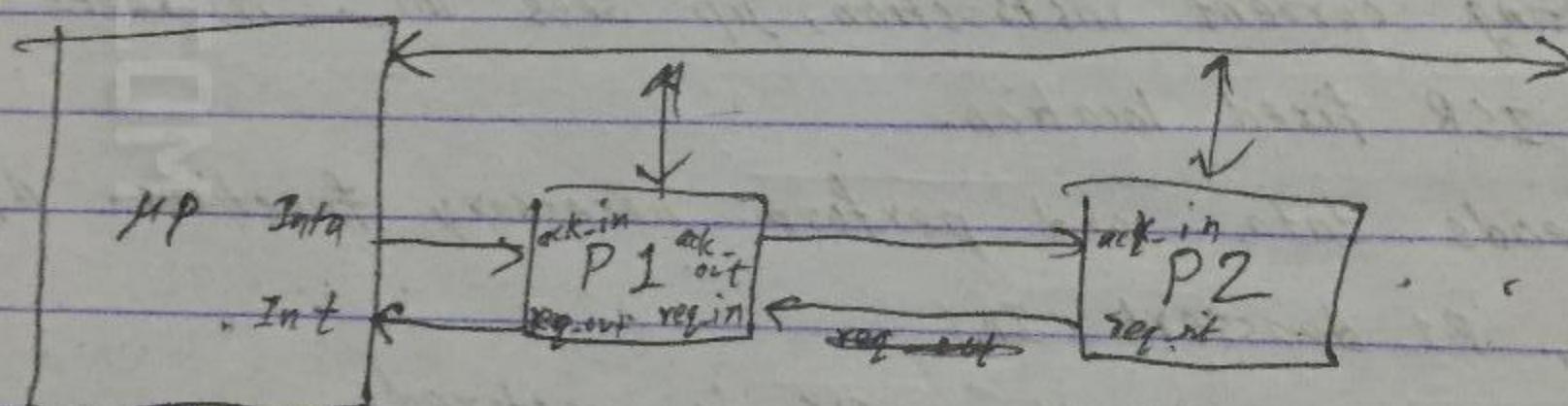
- μP gives control of system bus to DMA controller
- μP can execute its regular program.

### 5.5 Arbitration

- Priority Arbiter

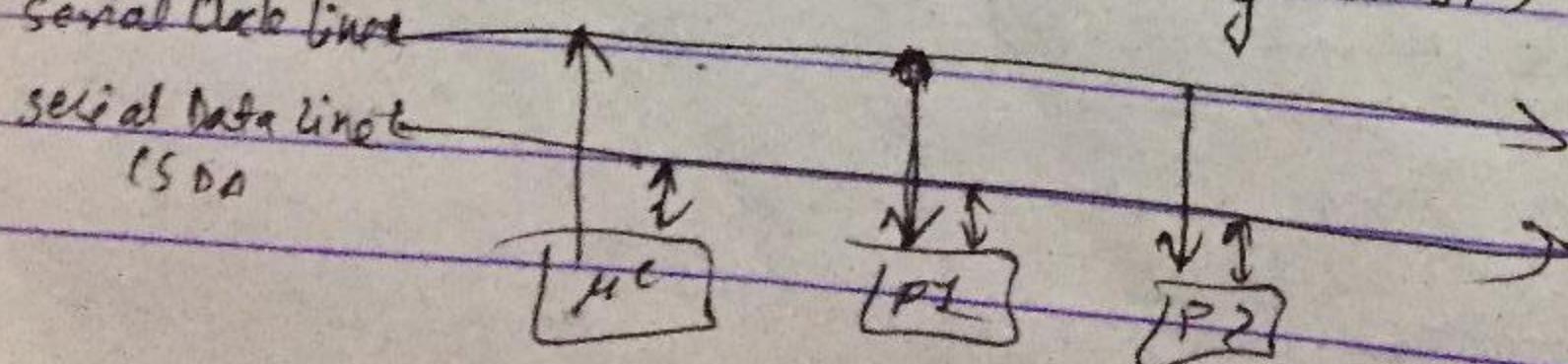


- Daisy-chain arbitration

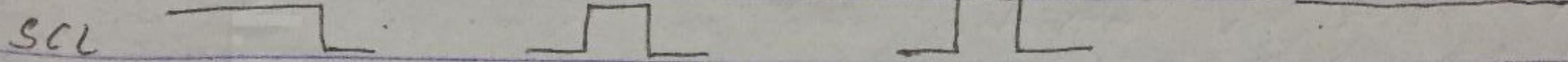
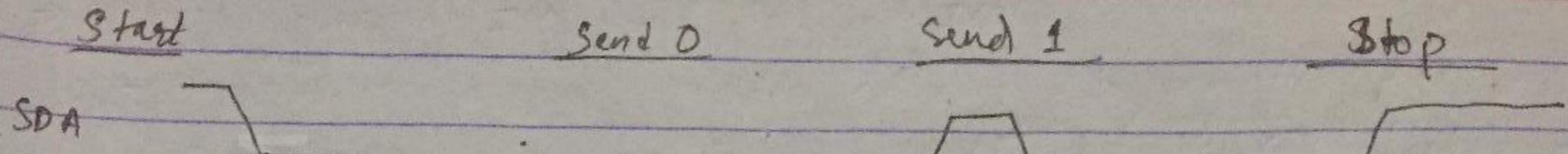


### → I<sup>2</sup>C Protocol

- Inter-I<sup>2</sup>C protocol
- Enable peripheral ICs to communicate.
- Data transfer rate upto 100 kbit/s & 7-bit addressing (normal)
- 3.4 Mbit/s & 10 bit addressing (fast)



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## Chapter 7 Control System

7.1 Open-loop and Close-loop control system

7.2 Control system and PID controller

7.3 Software coding of a PID controller

7.4 PID Tuning

### 7.1 Control System

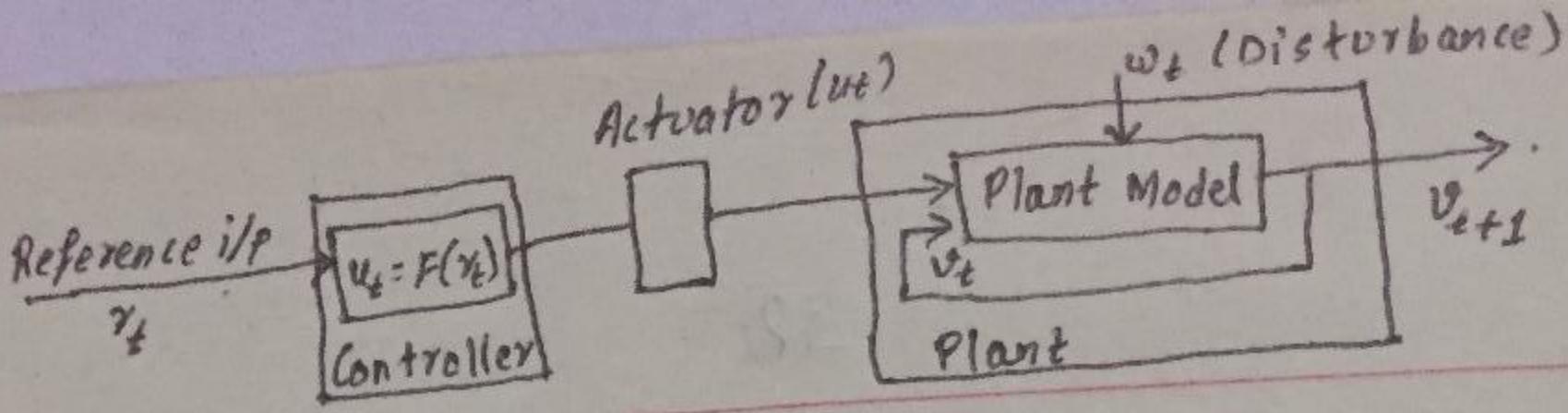
Control system is a system designed to control physical system's output to a desired limit by setting desired reference input.

→ Automobile Cruise Controller

This controller seeks to make a car's speed track a desired speed by setting the car's throttle and brake inputs.

→ Thermostat Controller

It forces a building's temp to a desired temp by turning on the heater or AC and adjusting the fan speed.



## 7.2 Open Loop Control System

→ It is a feed-forward control system

→ It consists of following parts:

→ Plant / Process

It is the physical system to be controlled.

→ Output

It is the particular aspect of physical system that we intend to control.

→ Reference input

It is the desired value that we want to see for the output.

→ Actuator

It is the device used to control i/p to the plant.

→ Controller

It is the system used to compute the i/p to the plant so as to achieve desired o/p.

→ Disturbance

It is an additional undesirable i/p imposed by environment that cause o/p to differ from our expectation.

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### 7.3 Designing Open Loop Control System

#### 7.3.1 Model of plant

Model of the plant is developed to make design phase easier and to derive the controller.

For eg: Throttle that goes from 0 to 95 degree

→ On flat surface at 50 mph, open throttle to 90 degree

→ Wait 1 "time unit"

→ Measure the speed, let's say 55 mph

→ Then, the equation that holds for all scenario gives model of the plant.

$$\text{i.e. } v_{t+1} = 0.7 * v_t + 0.5 * u_t$$

$$55 = 0.7 * 50 + 0.5 * 40$$

#### 7.3.2 Controller design

Controller provides a specific rule to achieve the goal of the control system.

For eg: Assume we use simple linear function.

$$u_t = F(r_t) = p * r_t$$

where,  $p$  = constant

$r_t$  = desired speed

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Now,

$$v_{t+1} = 0.7 * v_t + 0.5 * u_t = 0.7 * v_t + 0.5 * p * r_t$$

Let  $v_{t+1} = v_t$  at steady state =  $v_{ss}$ ;

$$v_{ss} = 0.7 * v_{ss} + 0.5 * p * r_t$$

At steady state, we want  $v_{ss} = r_t$

$$1 = 0.7 + 0.5 * p$$

$$\therefore p = 0.6$$

Hence, the control rule is defined as:

$$u_t = p * r_t = 0.6 * r_t$$

### 7.3.3 Analyzing Controller

Suppose  $v_0 = 20 \text{ mph}$  and  $r_0 = 50 \text{ mph}$

$$\text{Then, } v_{t+1} = 0.7 * v_t + 0.5 * 0.6 * r_t$$

$$= 0.7 * v_t + 0.3 * 50$$

$$= 0.7 * v_t + 15$$

$\therefore$  Throttle position =  $0.6 * 50 = 30 \text{ degree}$

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### 7.3.4 Considering Disturbance

Assume road grade affect speed from -5 mph to +5 mph.

| Time (t) | $v_t$ | $v_t (\omega = +5)$ | $v_t (\omega = -5)$ |
|----------|-------|---------------------|---------------------|
| 0        | 20    | 20                  | 20                  |
| 1        | 29    | 32                  | 34                  |
| 2        | 35.30 | 26.80               | 43.80               |
| 3        | 39.71 | 28.76               | 50.66               |
| 4        | 42.80 | 30.13               | 55.46               |
| 5        | 44.96 | 31.09               | 58.82               |
| 6        | 46.47 | 31.76               | 61.18               |
| 7        | 47.53 | 32.24               | 62.82               |
| 8        | 48.27 | 32.56               | 63.98               |
| 9        | 48.79 | 32.80               | 64.78               |
| 10       | 49.15 | 32.96               | 65.35               |
| 11       | 49.41 | 33.07               | 65.74               |
| 12       | 49.58 | 33.15               | 66.02               |

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### 3.3.5 Determining Performance

$$v_{t+1} = 0.7 v_t + 0.5 P r_0 - w_0$$

$$\therefore v_1 = 0.7 v_0 + 0.5 P r_0 - w_0$$

$$\begin{aligned}\therefore v_2 &= 0.7(0.7 v_0 + 0.5 P r_0 - w_0) + 0.5 P r_0 - w_0 \\ &= 0.7^2 v_0 + (0.7 + 1)(0.5 P r_0 - w_0)\end{aligned}$$

$$\therefore v_t = 0.7^t v_0 + (0.7^{t-1} + 0.7^{t-2} + \dots + 0.7 + 1)(0.5 P r_0 - w_0)$$

→ Coefficient of  $v_t$  determines rate of decay of  $v_0$

→ If  $> 1$  or  $< -1$ ,  $v_t$  will grow without bound

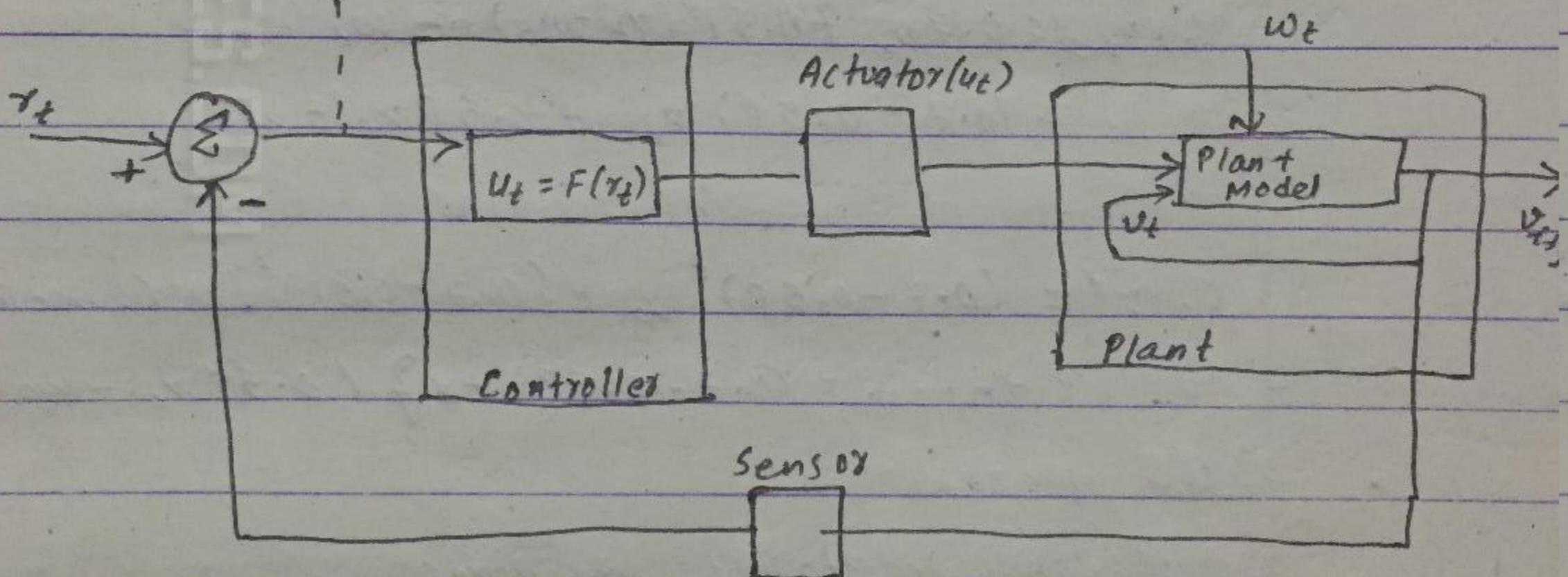
→ Otherwise,  $v_t$  will oscillate.

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### 7.4 Close Loop Control System

- It is a feedback control system
- It minimizes tracking error
- It consists of some additional part (sensors to measure plant output and error detector to detect errors).

$$e_t(\text{error}) = r_t - v_t$$



## 7.5 Designing Close Loop Control System

### 7.5.1 Design model of the plant

$$v_{t+1} = 0.7v_t + 0.5u_t - w_t$$

### 7.5.2 Design controller

$$u_t = P(r_t - v_t)$$

$$\therefore v_{t+1} = 0.7v_t + 0.5P(r_t - v_t) - w_t$$

$$= (0.7 - 0.5P)v_t + 0.5Pr_t - w_t$$

$$\therefore v^t = (0.7 - 0.5P)^t v_0 + \{(0.7 - 0.5P)^{t-1} + (0.7 - 0.5P)^{t-2} \\ + \dots + (0.7 - 0.5P)^1\}(0.5Pr_0 - w_0)$$

so,

Stability constraint requires :

$$|0.7 - 0.5P| < 1$$

$$\text{or, } -1 < 0.7 - 0.5P < 1$$

$$\therefore -0.6 < P < 3.4$$

### 7.5.3 Reducing effect of $v_0$

To reduce effect of initial condition (i.e.  $v_0$ )

a)  $0.7 - 0.5P$  must be as small as possible.

$$\text{i.e. } 0.7 - 0.5P = 0$$

$$\therefore P = 1.4$$

### 7.5.4 Avoid Oscillation

To avoid oscillation,  $(0.7 - 0.5P)$  must be greater than or equal to 0.

$$\text{i.e. } 0.7 - 0.5P \geq 0$$

$$\therefore P \leq 1.4$$

### 7.5.5 Perfect Tracking

Assume at steady state  $v_{ss}$ ,  $v_{t+1} = v_t$  ;

$$v_{ss} = (0.7 - 0.5P) v_{ss} + 0.5P\gamma_0 - w_0$$

$$\text{or, } (1 - 0.7 + 0.5P) v_{ss} = 0.5P\gamma_0 - w_0$$

$$\therefore v_{ss} = \frac{0.5P\gamma_0 - w_0}{0.3 + 0.5P} = \frac{0.5}{0.3 + 0.5P} \gamma_0 - \frac{1}{0.3 + 0.5P} w_0$$

→ To make  $v_{ss}$  close to  $\gamma_0$ ,  $P$  should be as large as possible

### 7.5.6 Analyse Controller

- Set  $P = 3.3$ , saturate at 0, 45. Oscillation
- Set  $P = 1$  to avoid oscillation, terrible SS performance.

## 7.6 General Control System

### 1) P controller

→ It multiplies the tracking error by a constant.

$$\rightarrow u_t = P(r_t - v_t)$$

→ P affects transient response (stability), steady state tracking error and disturbance rejection.

### 2) PD controller

→ It considers the size of error over time.

→ It keep track of error derivative.

$$\rightarrow u_t = P * e_t + D * (e_t - e_{t-1})$$

→ P set for best tracking and disturbance control.

→ D set to control oscillation and convergence rate.

### 3) PI controller

→ It sum up error over time

$$\rightarrow u_t = P * e_t + I * (e_0 + e_1 + \dots + e_t)$$

→ P controls disturbance

→ I ensures steady state convergence.

### 4) PID controller

→ Combines proportional, integral and derivative control.

$$\rightarrow u_t = P * e_t + D * (e_t - e_{t-1}) + I * (e_0 + e_1 + \dots + e_t)$$

→ It achieves desired stable transient behavior.

### 7.7 Software Coding for PID controller

```
void main()
```

```
{
```

```
 double sen-val, act-val, err-current;
```

```
PID- DATA pid-data;
```

```
PidInitialize (&pid-data);
```

```
while (1)
```

```
{
```

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sen-val = SensorGet Value();

ref-value = Reference Get Value();

act-value = PidUpdate (&pid-data, sen-val, ref-val);

Actuator Set Value (act-value);

}

{

typedef struct PID- DATA {

double Pgain, Dgain, Igain;

double sen-val-previous; // find derivative

double error-sum; // cumulative error

}

double PidUpdate (PID- DATA \*pid-data, double sen-val,  
double ref-val)

{

double Pterm, Iterm, Dterm;

double err, diff;

err = ref-val - sen-val;

Pterm = pid-data -> Pgain \* err;

`pid-data->error_sum += error;`

`Iterm = pid-data->Igain * pid-data->error-sum;`

`diff = pid-data->sen_val_previous - sen_val;`

`pid-data->sens_val_previous = sen_val;`

`Dterm = pid-data->Dgain * diff;`

`return (Pterm + Iterm + Dterm);`

`}`

## 7.8 PID Tuning

→ PID tuning is the process of obtaining P, I and D by ad-hoc methods.

→ It is necessary because:-

a) With analytics, the plant model may be complex.

b) We may not even have a plant model.

→ Algorithm

1) Start with a small P, I = D = 0

2) Increase D, until seeing oscillation.

→ Decrease D a bit.

3) Increase P, until seeing oscillation

→ Decrease P a bit

4) Increase I, until seeing oscillation

5) Repeat from 2 until performance can not be further improved.

## 7.9 Issues with Computer Based Control

### 1) Quantization and Overflow

- Quantization occurs when a signal must be altered to fit memory constraints.
- Arithmetic operations cause quantization.
- Eg: Assume an operation results 0.36 but it can not be stored as 4-bit fractional number. So, 0.25 is chosen.

→ Overflow occurs when operation outputs a number with magnitude too large to be represented by a processor.

- Use fix point representation carefully (time consuming)
- Use floating-point co-processor (expensive)

### 2) Aliasing

- Aliasing is due to the discrete nature of sampling.
- Eg: Sampling at 2.5 Hz, period of 0.4;

$$y(t) = 1.0 * \sin(6\pi t), f = 3 \text{ Hz}$$

$$y(t) = 1.0 * \sin(\pi t), f = 0.5 \text{ Hz}$$

They are indistinguishable.

### 3) Computational Delay

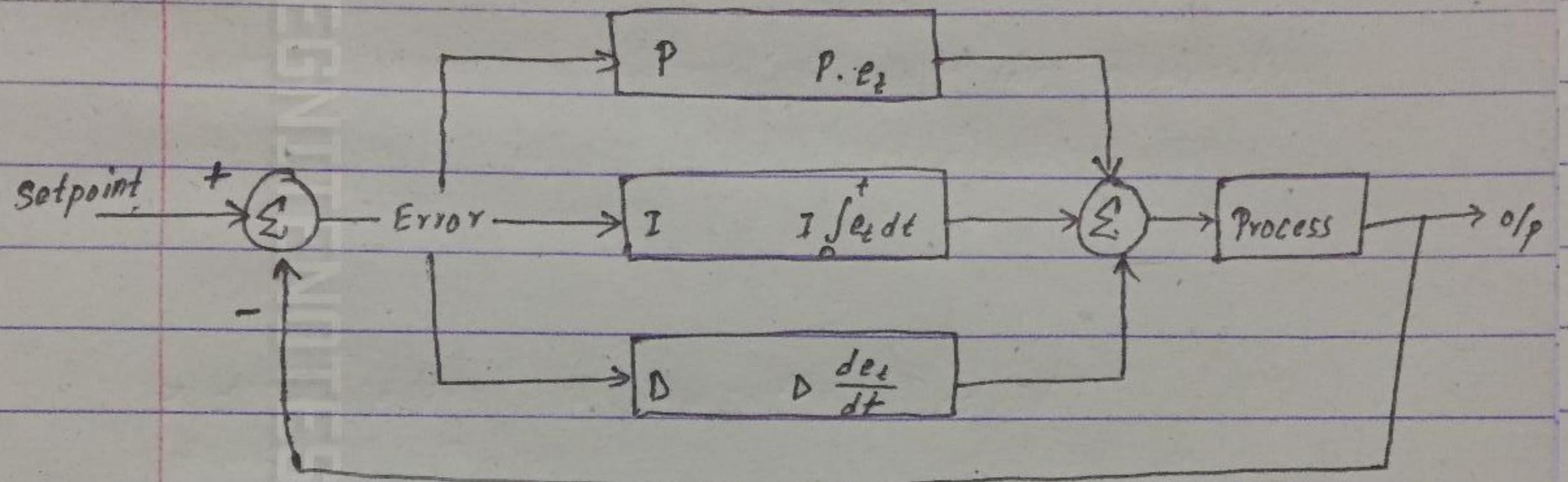
- The computation causes delay to occur that causes actuation to delay.
- The implementation delay must be negligible.
- Software delay is hard to predict.

### 7.10 Benefits of Computer Control

- 1) Cost
- 2) Programmability
- 3) Reproducible

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Q) Block Diagram of PID.



## Chapter 8 IC Technology

8.1 Full Custom (VLSI) IC Technology

8.2 Semi Custom (ASIC) IC Technology

8.3 Programming Logic Device (PLD) IC Technology

### 8.1 IC Manufacturing Steps

IC is a semiconductor wafer in which various active and passive components along with external connections are fabricated in extremely tiny silicon chip

The various steps for IC manufacturing are as follows:-

1) Wafer Production

2) Photolithography

3) Doping

4) Metallization

5) Assembly and packaging

## 1) Wafer Production

Wafer is a round slice of semiconductor material such as silicon. In IC, silicon wafer is used.

- Purified polycrystalline Si is created from sand.
- It is heated to produce molten liquid.
- A small piece of solid Si is dipped into molten liquid.
- Solid silicon is slowly pulled from the melt.
- The liquid cools to form single crystal.
- A thin round wafer is cut using wafer slicer.
- The wafer surface is smoothened by polishing.
- It is cleaned and dried using high purity low particle chemicals.

## 2) Photolithography

Photolithography is the process of printing a pattern of mask into the silicon wafer. It is carried out using light sensitive photoresist and controlled exposure to light.

Positive photolithography prints a pattern that is same as the pattern on the mask.

Negative photolithography prints a pattern that is opposite of the pattern as that on the mask.

### 3) Doping

To alter electrical character of silicon, atom with one less electron and atom with one more electron are introduced in to the area. The impurity atoms in semiconductor material are moved at high temperature.

### 4) Metallization

It is used to create contact with Si and to make interconnections on chip. A thin layer of aluminum is deposited over the wafer.

### 5) Assembly and packaging

Each wafer consists of many chips. These chips are separated and packaged by scribing and cleaving.

A diamond saw is used to cut wafer into chips. The tested and verified chip is mounted into a package. It is encapsulated for protection.

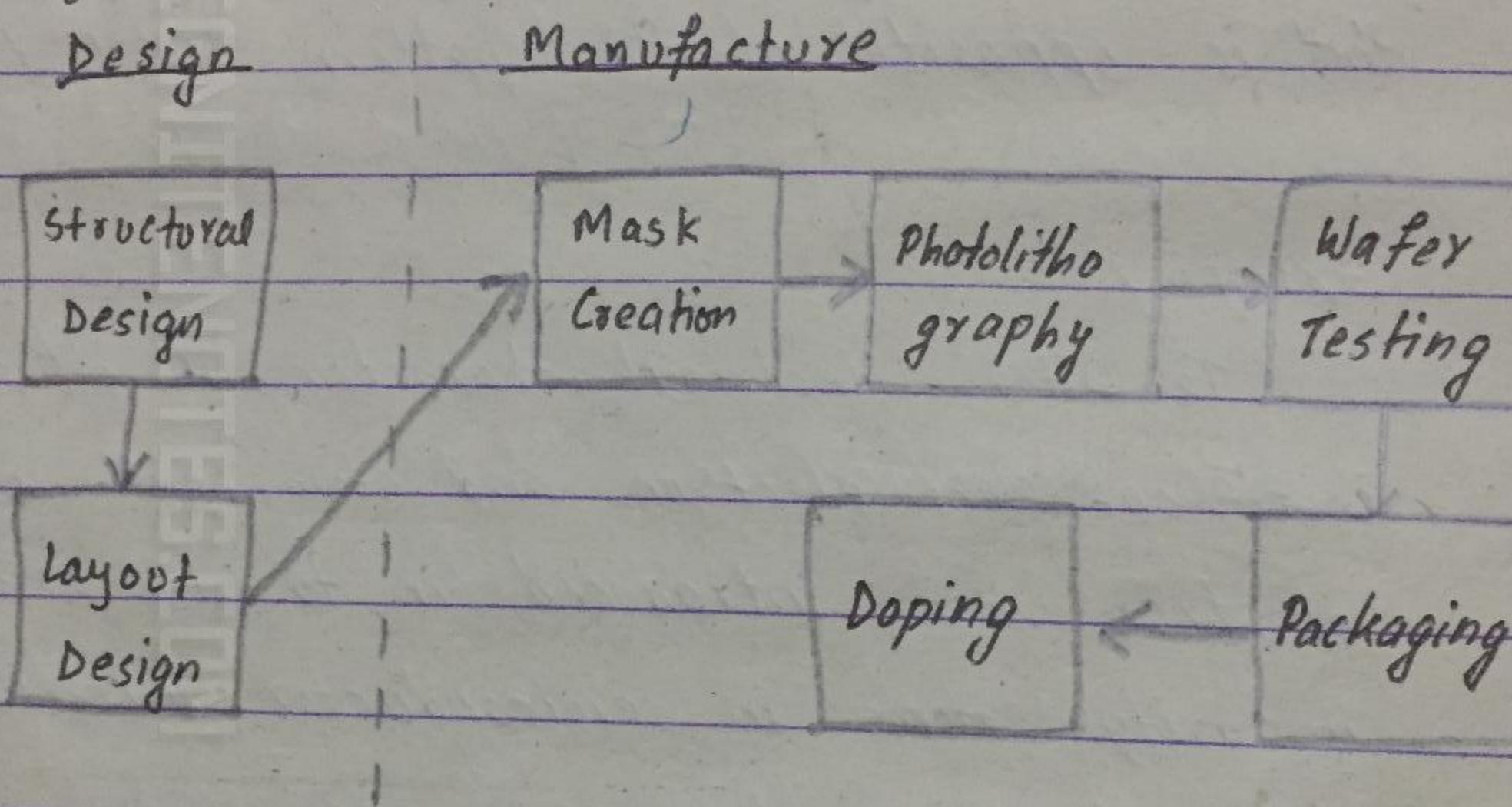


Fig. IC Manufacturing Steps

→ Wafer condition before

- 1) Surface includes film composition, bare surface and reflectivity.
- 2) It affects:
  - a) photoresist -to- wafer adhesion
  - b) alignment accuracy
  - c) linewidth resolution
  - d) exposure settings
  - e) bake time

→ Wafer condition after

- a) resist coated wafer
- b) patterned resist layer
- c) withstand etching
- d) withstand ion implanting

## → Steps of Photolithography

### 1) Surface Preparation

- It increases adhesion of photoresist material to the substrate.
- Dehydration bake removes water from substrate by baking at temp. of  $200^{\circ}\text{C}$  to  $400^{\circ}\text{C}$  for 30 to 60 minutes
- The substrate is then cooled and coated.
- Adhesion promoters like Hexamethyl disilizane (HMDS) are used to react chemically with surface and replace -OH with organic function group.

### 2) Photoresist Coating

- A thin uniform coating of photoresist is accomplished by spin coating.
- The photoresist in liquid form is poured onto the wafer and then spun at a high speed to produce desired film.
- Thickness is affected by spin speed, time and volume of resist.

### 3) Soft Bake

- The film contain about 20-40% by weight solvent.
- It involves drying or removing of excess solvent.
- It helps to stabilize the resist film.
- It improves adhesion and uniformity
- It is baked in oven at 95°C for 30 mins.

### 4) Alignment and Exposure

- A photo mask with pattern on one side is aligned over the wafer.
- A UV light (12mW) is exposed to the surface.
- It transfers the mask image to the resist coated wafer.
- The exposure time affects critical dimension. With increase in expose time, CD increase.

### 5) Develop

- Soluble areas of photoresist are dissolved by developer chemical.
- A visible patterns appear on wafer.

### 6) Hard bake

→ It hardens the final resist image.

→ Hard bake is done at temp. of  $110^{\circ}\text{C}$  for about 30 minutes.

→ It improves adhesion.

### 7) Develop inspection

→ The resist patterned wafer is inspected for particles, defects, CD, linewidth resolution and overlay accuracy.

### 8) Etching

→ It is the selective removal of upper layer of wafer.

→ It is performed either by using wet chemicals (acids) or in a dry plasma environment.

### 9) Strip

→ It is the process of removing photoresist.

→ Wet acid strip or dry plasma strip.

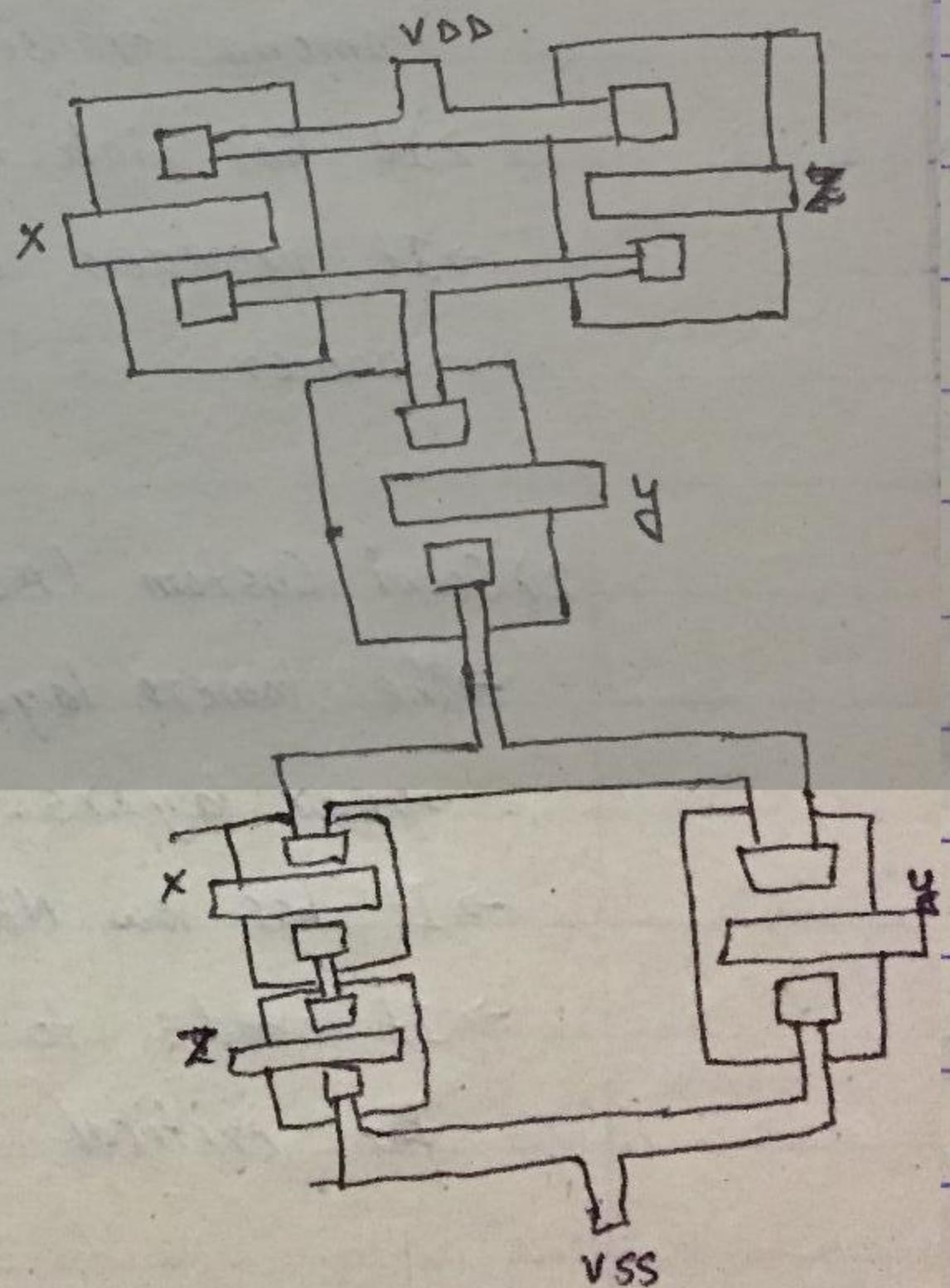
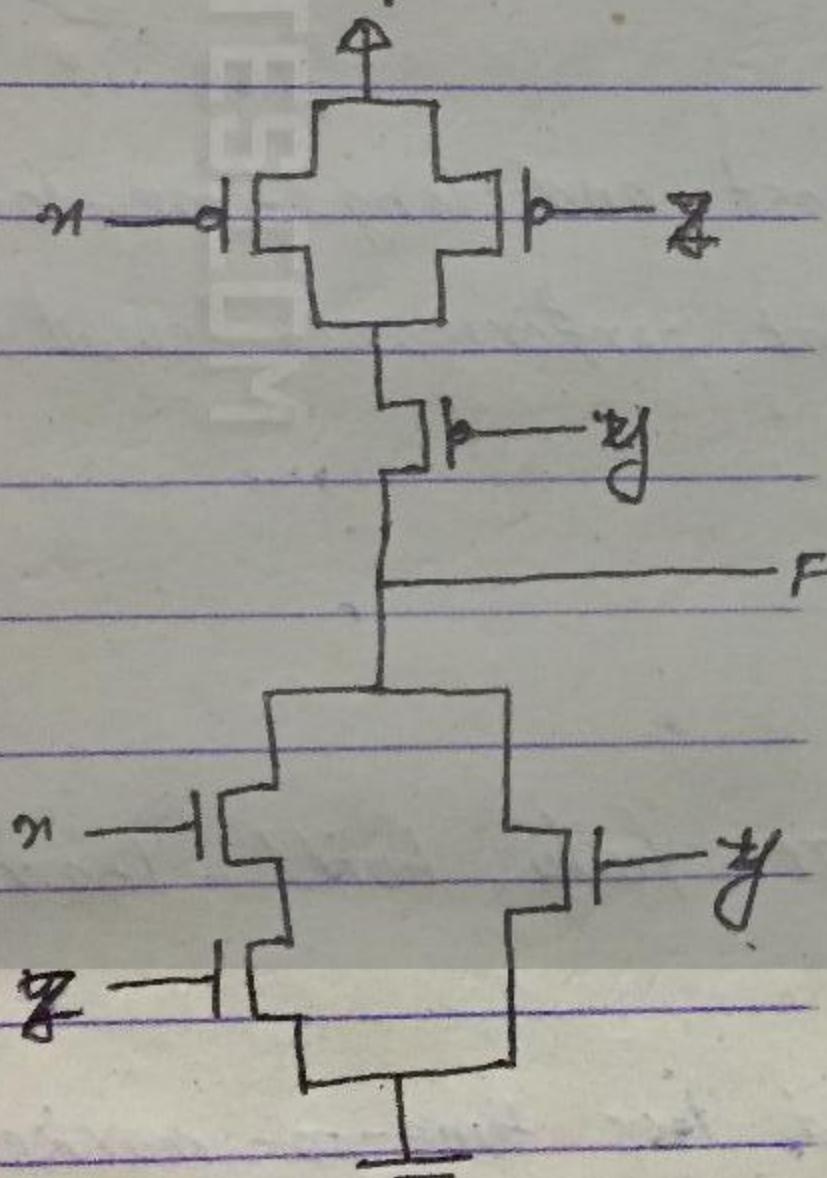
## 10) Final Inspection

→ Complete removal of photo resist.

→ Pattern on wafer to be correct.

→ Defects, particles, step height and CD are checked.

Q. Show top-down view of circuit  $F = \bar{u}zty$  on an IC.



### 3.2 Types of IC Technology

#### 1) Full Custom (VLSI)

- All layers are optimized for a particular ES implementation.
- It involves placement of transistors to minimize interconnection length, sizing transistor to optimize signal transmission and routing wires among transistors.
- It has high NRE cost and long time-to-market.
- It provides excellent performance, small size and power.

#### 2) Semi Custom (ASIC)

- The lower layers are fully built leaving the upper layers.
- It has low NRE and less time-to-market.
- It needs to integrate with full custom IC for critical regions of design.

### 3) Programming Logic Device (PLD)

- All layers already exists with a programmable circuit.
- It involves creation or destruction of connection between wires that connect gates.
- It has very low NRE and instant time-to-market.
- FPGA is a complex PLD that offers general connectivity among blocks of logic.

## Chapter 9

### 8051 Microcontroller

1) Continuously toggles the value of port 0.

```
#include<reg51.h>
void main(void)
{
 while(1)
 {
 P0 = 0X00;
 Assembly
 P0 = 0xFF;
 }
}
```

loop: MOV A, #00H

MOV P0, A

MOV A, #0FFH

MOV P0, A

SJMP loop

P0 = 0X00;

P0 = 0xFF;

2) Get data from P0 and set to P1.

```
#include<reg51.h>
```

```
void main(void)
```

```
{ P0 = 0xFF;
P1 = 0x00;
```

```
while(1)
```

```
{
```

```
P1 = P0;
```

```
}
```

```
MOV A, #0FFH
```

```
MOV P0, A
```

```
MOV A, #00H
```

```
MOV P1, A
```

```
loop: MOV A, P0
```

```
MOV P1, A
```

```
SJMP loop
```

```
?
```

3) Create 50% duty cycle on bit 0 of port 1.

```
#include<reg51.h>
sbit mybit = P1^0;
void delay(unsigned int n)
{
 unsigned int x, y;
 x = 0;
 y = 0;
 while(x < n)
 {
 while(y < 2275)
 {
 y++;
 }
 x++;
 }
}
void main(void)
{
 while(1)
 {
 mybit = ~mybit;
 delay(250);
 }
}
```

loop: SETB P1.0  
       LCALL DELAY  
       CLR P1.0  
       LCALL DELAY  
       SJMP loop

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4) Get status of switch at P1.0 and sent it to LED at  
P2.7

#include <reg51.h>

SETB P1.0

sbit in-bit = P1^0;

CLR P2.7

sbit out-bit = P2^7;

loop: MOV A, P1.0

void main(void)

MOV P2.7, C

{

SJMP loop

while (1)

{

out-bit = in-bit;

}

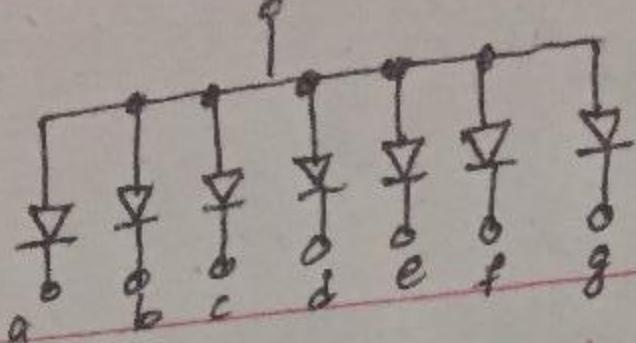
}

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5> Blink 8 LEDs connected at Port 2.

```
#include <reg51.h> MOV A, #00H
void main(void) MOV P2, A
{
 P2 = 0X00; loop: MOV A, #00H
 MOV P2, A
 while(1) MOV A, #0FFH
 MOV P2, A
 P2 = 0X00; SJMP loop
 P2 = 0XFF;
}
```

Common  
Anode



ON  $\rightarrow 0$       f | a | b  
OFF  $\rightarrow 1$       e | g | c  
                        d

6) 7 segment display to show 0 to 9.

MOV A, #00H

#include <reg51.h>

MOV P2, A

void main(void)

{ P2 = 0X00;

MOV P2, #C0

P2 = 0XCO;

ACALL DELAY

Delay (200);

MOV P2, #F9

P2 = 0XF9;

ACALL DELAY

Delay (200);

MOV P2, #A4

P3 = 0XA4;

Delay (200);

ACALL DELAY

MOV P2, #B0

ACALL DELAY

MOV P2, #99

?

ACALL DELAY

MOV P2, #92

ACALL DELAY

MOV P2, #82

ACALL DELAY

MOV P2, #F8

ACALL DELAY

MOV P2, #80

ACALL DELAY

MOV P2, #90

ACALL DELAY

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7) 7 segment display to show 99 to 00.

```
#include <reg51.h>
void main (void)
{
 int i, j;
 int array[10];
 array[0] = 0xED;
 array[1] = 0xF9;
 array[2] = 0xA4;
 array[3] = 0xB0;
 array[4] = 0x99;
 array[5] = 0x92;
 array[6] = 0x82;
 array[7] = 0xF8;
 array[8] = 0x80;
 array[9] = 0x90;
 P1 = 0x00;
 P2 = 0x00;
 for (i=9; i>=0; i--)
 {
 P2 = array[i];
 for (j=9; j>=0; j--)
 {
 P2 = array[j];
 P1 = P2;
 }
 }
}
```

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8) Sum of two 8-bit BCD in RAM at 50H and 51H  
and store BCD sum at RAM 52H and 53H.

MOV R0, #50H

#include <reg51.h>

MOV A, 50H

void main(void)

MOV B, 51H

{

CLR R7

P0 = 0X50;

ADD A, B

P1 = 0X51;

DA A

JNC next

INC R7

next: MOV 52H, R7

MOV 53H, A

A) Compute precise 5-ms delay.

For 5ms;

$$n \times 1.085 \mu s = 5 \text{ ms} \quad 1 + (65535 - 4608) = 60927 + 1$$

$$\therefore n = 4608 = \cancel{9608H} \quad = EE00H$$

$$\Rightarrow FFFF - n = 9608 \Rightarrow n = \underline{\underline{637F}}$$

```
#include <reg51.h>
```

```
void delay(void);
```

```
void main(void)
```

```
{ while(1)
```

```
S
```

```
DELAY: MOV TMOD, #01
```

```
delay();
```

```
here: MOV TL0, #0
```

```
?
```

```
MOV TH0, #0EEH
```

```
?
```

```
SETB TR0
```

```
void delay(void)
```

```
again JNB TF0, again
```

```
{ TMOD = 0X01;
```

```
CLR TR0
```

```
TL0 = 0X00;
```

```
CLR TF0
```

```
TH0 = 0X EE;
```

```
TR0 = 1;
```

```
while (TF0 == 0);
```

```
TR0 = 0;
```

```
TF0 = 0;
```

```
3
```

# Common Anode 7-Segment Display

|   | a | b | c | d | e | f | g |   |      |
|---|---|---|---|---|---|---|---|---|------|
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | = CO |
| 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | = FG |
| 2 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | = AG |
| 3 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | = BO |
| 4 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | = 99 |
| 5 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | = 92 |
| 6 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | = 82 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | = F8 |
| 8 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | = 80 |
| 9 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | = 90 |

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Chapter - 10  
VHDL

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1) NOT Gate

X F

library ieee;

0 1

use ieee.std\_logic\_1164.all;

1 0

ENTITY not1 IS

PORT ( n : IN STD\_LOGIC;

F : OUT STD\_LOGIC;

);

END not1;

ARCHITECTURE behv1 OF not1 IS

BEGIN

PROCESS(x)

BEGIN

IF (x = '1') THEN

F <= '0';

ELSE

F <= '1';

END IF;

END PROCESS;

END behv1;

2) OR Gate

library ieee;

use ieee.std\_logic\_1164.all;

ENTITY or2 IS

PORT ( x, y : IN STD\_LOGIC;

      F : OUT STD\_LOGIC;

);

END or2;

ARCHITECTURE behv1 OF or2 IS

BEGIN

process (x, y)

BEGIN

IF ((x = '0') AND (y = '0')) THEN

    F <= '0';

ELSE

    F <= '1';

ENDIF;

END process;

END behv1;

| X | Y | F |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

## 3) AND Gate

```
library ieee;
```

```
use ieee.std_logic_1164.all;
```

```
ENTITY and2 IS
```

```
PORT (x, y : IN STD-LOGIC;
```

```
 F : OUT STD-LOGIC;
```

```
);
```

```
END and2;
```

```
ARCHITECTURE behav1 OF and2 IS
```

```
BEGIN
```

```
process (x, y)
```

```
 BEGIN
```

```
 IF ((x='1') AND (y='1')) THEN
```

```
 F <= '1';
```

```
 ELSE
```

```
 F <= '0';
```

```
 END IF;
```

```
 END process;
```

```
END behav1;
```

| X | Y | F |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

\*> XOR Gate

library ieee;

use ieee.std\_logic\_1164.all;

ENTITY nor2 IS

PORT (x, y: IN STD\_LOGIC;

F : OUT STD\_LOGIC;

);

END nor2;

| x | y | F |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

ARCHITECTURE behv1 OF nor2 IS

BEGIN

process (x, y)

BEGIN

IF ((x='0') AND (y='0')) THEN

F &lt;= '0' ;

ELSE IF ((x='1') AND (y='1')) THEN

F &lt;= '0' ;

ELSE

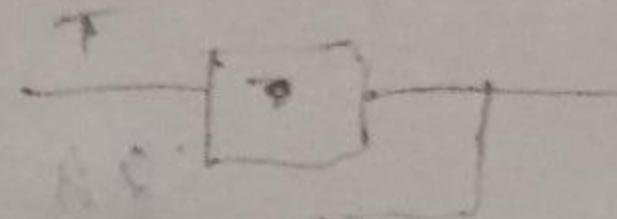
F <= ~~'0'~~ '1' ;

END IF;

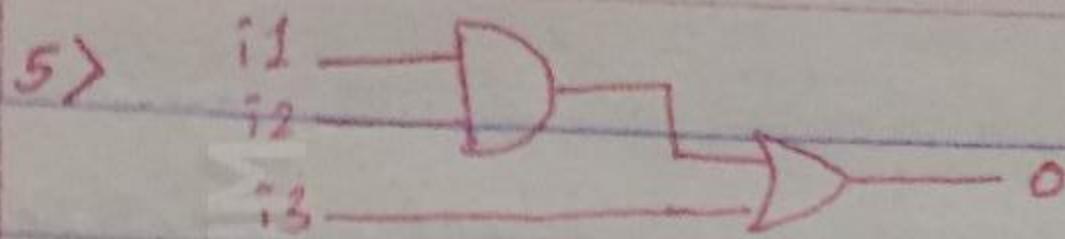
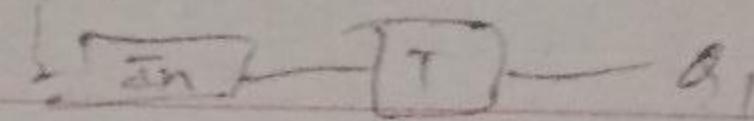
END process;

END behv1;

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O.



-- component 1

library ieee;

use ieee.std\_logic\_1164.all;

ENTITY OR2 IS

PORT (X, Y : IN STD\_LOGIC;

F1 : OUT STD\_LOGIC;

);

END OR2;

ARCHITECTURE behv1 OF OR2 IS

BEGIN

process (X, Y)

BEGIN

IF ((X = '0') AND (Y = '0'))

F1 &lt;= '0';

ELSE

F1 &lt;= '1';

END IF;

END process;

END behv1;

```
-- component 2
library ieee;
use ieee.std_logic_1164.all;
ENTITY and2 IS
PORT (A,B : IN STD-LOGIC;
 F2 : OUT STD-LOGIC;
);
END and2;
ARCHITECTURE behv2 OF and2 IS
BEGIN
process (A,B)
BEGIN
 F2 <= A AND B;
END process;
END behv2;
```

-- Top level circuit

library ieee;

use ieee.std\_logic\_1164.all;

use work.all;

ENTITY comb\_ckt IS

PORT (i1, i2, i3 : IN STD-LOGIC;

o : OUT STD-LOGIC;

);

END comb\_ckt;

ARCHITECTURE behv OF comb\_ckt IS

COMPONENT and2 IS

PORT (A, B : IN STD-LOGIC;

F2 : OUT STD-LOGIC;

);

END COMPONENT;

COMPONENT or2 IS

PORT (X, Y : IN STD-LOGIC;

F1 : OUT STD-LOGIC;

);

END COMPONENT;

SIGNAL wire : STD-LOGIC;

BEGIN

Gate1 : and2 PORT MAP (A=>i1, B=>i2, F2=>wire);

Gate2 : or2 PORT MAP (x=>wire, y=>i3, F1=>0);

END behv;

6) MUX

ENTITY mux IS

PORT (I3, I2, I1, I0 : IN STD\_LOGIC\_VECTOR (2 DOWNTO 0)

S : IN STD\_LOGIC\_VECTOR (1 DOWNTO 0);

O : OUT STD\_LOGIC\_VECTOR (2 DOWNTO 0);

);

END mux;

ARCHITECTURE behv OF mux IS

BEGIN

process (I3, I2, I1, I0, S)

BEGIN

CASE S IS

WHEN "00" => O <= I0;

WHEN "01" => O <= I1;

WHEN "10" => O <= I2;

WHEN "11" => O <= I3;

WHEN OTHERS => O <= "ZZZ";

END CASE;

END process;

END behv;

## 7) DECODER

ENTITY Decoder IS

PORT (I : IN STD\_LOGIC\_VECTOR (2 DOWNTO 0)

O : OUT STD\_LOGIC\_VECTOR (3 DOWNTO 0)

);

END decoder;

ARCHITECTURE behv OF decoder IS

BEGIN

process (I)

BEGIN

CASE I IS

WHEN "00" =&gt; O &lt;= "0001";

WHEN "01" =&gt; O &lt;= "0010";

WHEN "10" =&gt; O &lt;= "0100";

WHEN "11" =&gt; O &lt;= "1000";

WHEN OTHERS =&gt; O &lt;= "2222";

END CASE;

END process;

END behv;

## 8&gt; ADDER

ENTITY adder IS

GENERIC (n : natural := 2);

PORT ( A, B : IN STD-LOGIC-VECTOR (n-1 DOWNTO 0);

C : OUT STD-LOGIC;

S : OUT STD-LOGIC-VECTOR (n-1 DOWNTO 0));

);

END adder

ARCHITECTURE behv OF adder IS

SIGNAL temp : STD-LOGIC-VECTOR (n DOWNTO 0);

BEGIN

temp &lt;= ('0' &amp; A) + ('0' &amp; B);

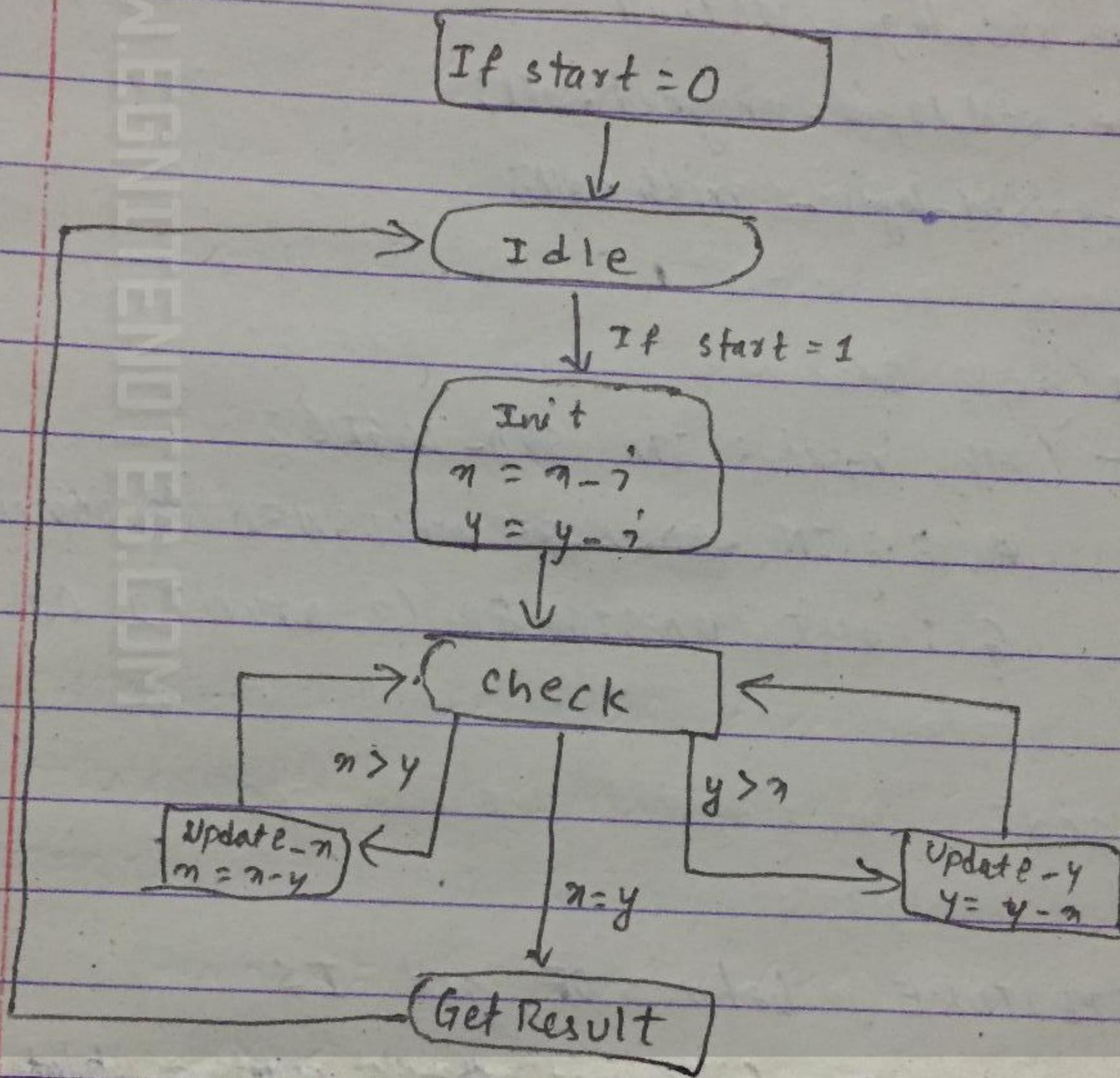
so S &lt;= temp (n-1 DOWNTO 0);

C &lt;= temp (n);

END behv;

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e) Calculate GCD



```

library ieee;
use ieee.std_logic_1164.all;
use ieee.std_logic_unsigned.all;
use ieee.std_logic_arith.all;

ENTITY gcd IS
PORT (clk, reset : IN STD_LOGIC;
 A, B : IN STD-LOGIC UNSIGNED (3 DOWNTO 0);
 G : OUT UNSIGNED (3 DOWNTO 0)
);
END gcd;

ARCHITECTURE behv OF gcd IS
TYPE state IS (idle, init, check, update_n, update_q, get-result);
SIGNAL pr-state : state := idle;
SIGNAL n-state : state;
SIGNAL start : STD_LOGIC := '1';

BEGIN

```

sequential: process (clk, reset) IS  
 BEGIN  
 IF (reset = '1') THEN  
 pr-state <= idle;  
 ELSE IF (clk = '1') THEN  
 pr-state <= n-state;  
 END IF;  
 END process sequential;

combinational: process (pr-state, A, B) IS  
~~BEGIN~~

variable tempx, tempy : UNSIGNED(3 DOWNTO 0); := '0000';  
 BEGIN  
 CASE pr-state IS  
 WHEN idle =>  
 IF (start = '1') THEN  
 n-state <= init;  
 start <= '0';  
 ELSE  
 n-state <= idle;  
 END IF

WHEN init =>

temp<sub>n</sub> := A;

temp<sub>y</sub> := B;

n-state <= check;

WHEN check =>

IF (temp<sub>n</sub> = temp<sub>y</sub>) THEN

n-state <= get-result;

ELSE IF (temp<sub>n</sub> > temp<sub>y</sub>) THEN

n-state <= update-n;

ELSE

n-state <= update-y;

ENDIF

WHEN update-n =>

temp<sub>n</sub> := temp-n + temp<sub>y</sub>;

n-state => check;

When update-y =>

temp<sub>y</sub> := temp<sub>y</sub> - temp<sub>n</sub>;

n-state => check;

When get-result =>

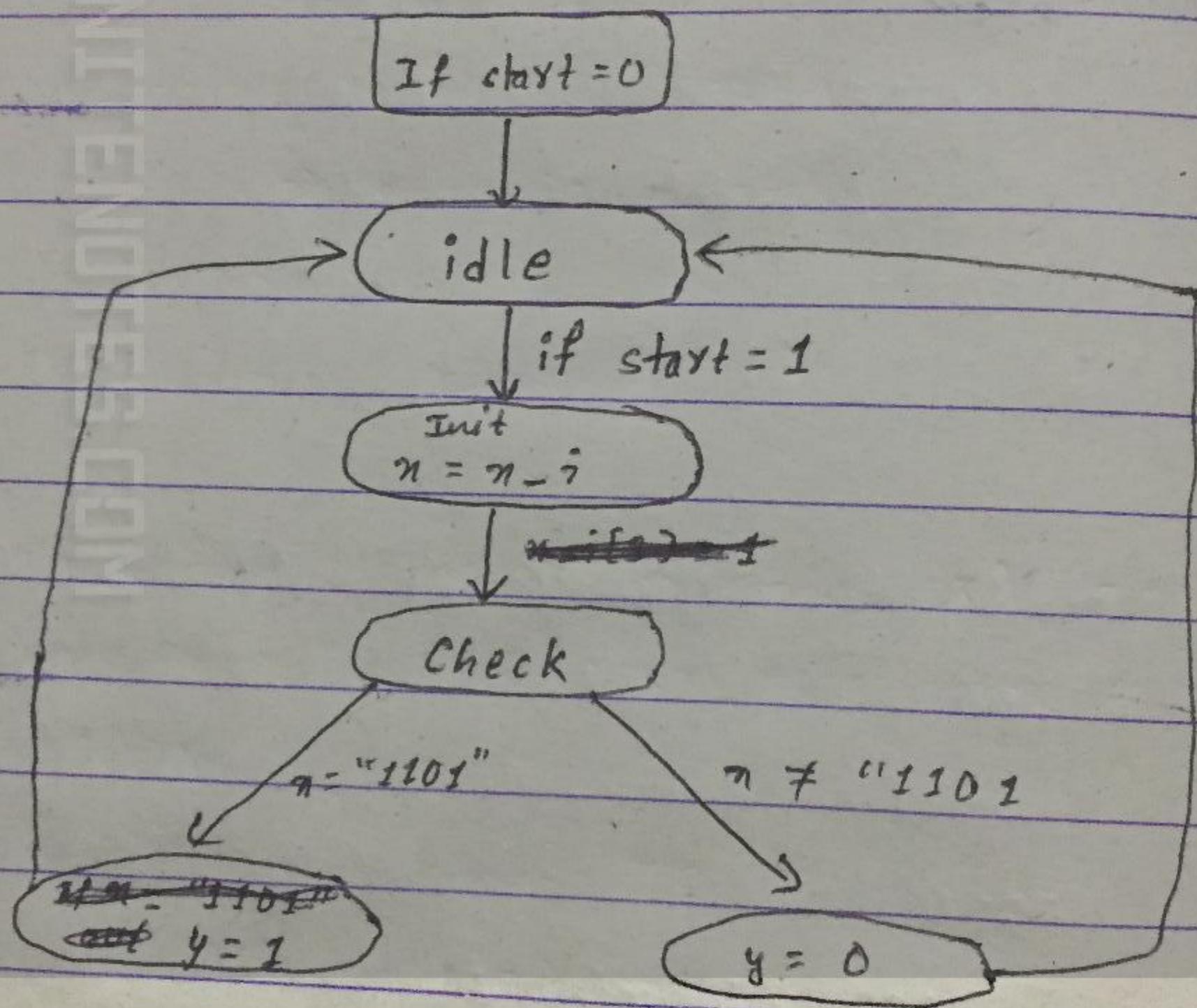
G <= temp<sub>n</sub>;

n-state <= idle;

90.

```
start <= '1';
END CASE;
END process combinational;
END behav;
```

10) Sequence Detector for string "1101", that outputs '1' when input matches the string.



```
library ieee;
use ieee.std_logic_1164.all;
use std_logic_arith.all;
use std_logic_unsigned.all;
```

```
ENTITY seq-det IS
PORT (x : IN STD-LOGIC-VECTOR (3 DOWNTO 0);
 y : OUT STD-LOGIC;
 clk : IN STD-LOGIC;
 reset : IN STD-LOGIC);

```

;

```
END seq-det;
```

```
ARCHITECTURE behv OF seq-det IS
```

```
TYPE state IS (idle, init, check, pos-out, neg-out);
SIGNAL pr-state : state := idle;
SIGNAL n-state : state;
SIGNAL start : STD-LOGIC := '1';
```

```
BEGIN
```

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sequential : process (clk, reset) IS

BEGIN

IF (reset = '1') THEN

pr-state <= idle;

ELSE IF (clk = '1') THEN

pr-state <= n-state;

ENDIF;

END process sequential;

combinational : process (pr-state, x) IS

~~variable~~ variable temp\_n : STD\_LOGIC\_VECTOR (3 DOWNTO 0);

BEGIN

CASE pr-state IS

WHEN idle =>

IF (start = '1') THEN

n-state <= init;

start <= '0';

ELSE

n-state <= idle;

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WHEN init =>

tempX <= X0;

n-state <= check;

WHEN check =>

IF (tempn = "1101") THEN

y <= '1';

~~END~~

ELSE

y <= '0';

END IF

n-state <= idle;

start <= '1';

END CASE;

END process combinational;

END behv;

## 1.1) T- FLIP FLOP

```
library ieee;
use ieee.std_logic_1164.all;
```

```
ENTITY t_ff IS
PORT (T : IN STD_LOGIC;
 clk : IN STD_LOGIC;
 Q : OUT STD_LOGIC);
END t_ff;
```

ARCHITECTURE behv OF t\_ff IS

SIGNAL tmp : STD\_LOGIC;

BEGIN

process (clk)

BEGIN

IF clk = '1' THEN

IF T = '0' THEN

tmp <= tmp;

ELSE

tmp <= NOT (tmp);

END IF;

END IF;

END process;

| T | Q | Qnext |
|---|---|-------|
| 0 | 0 | 0     |
| 0 | 1 | 1     |
| 1 | 0 | 1     |
| 1 | 1 | 0     |

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$A \leq \text{temp};$

END behv;

12) JK Flip Flop

| $J$ | $K$ | $Q_{\text{next}}$ |
|-----|-----|-------------------|
|-----|-----|-------------------|

|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
|---|---|---|

|   |   |   |
|---|---|---|
| 0 | 0 | 1 |
|---|---|---|

|   |   |   |
|---|---|---|
| 0 | 1 | 0 |
|---|---|---|

|   |   |   |
|---|---|---|
| 0 | 1 | 1 |
|---|---|---|

|   |   |   |
|---|---|---|
| 1 | 0 | 0 |
|---|---|---|

|   |   |   |
|---|---|---|
| 1 | 0 | 1 |
|---|---|---|

|   |   |   |
|---|---|---|
| 1 | 1 | 0 |
|---|---|---|

|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
|---|---|---|

13) D Flip Flop

$Q = D$

14) SR Flip Flop

$S = 0, R = 0; Q_n = Q$

$S = 1, R = 1; Q_n = Q$   
known

$S = 0, R = 1; Q_n = 0$

$S = 1, R = 0; Q_n = 1$

$J = 0, K = 0; Q_n = Q$

$J = 1, K = 1; Q_n = \bar{Q}$

$J = 0, K = 1; Q_n = 0$

$J = 1, K = 0; Q_n = 1$